

Reheating metastable SUSY-breaking sectors

Nathaniel Craig

SLAC, Stanford University

NC, Patrick Fox, Jay Wacker

hep-th/0611006; PRD 075, 085006 (2007)

Related work:

Abel et al., hep-th/0610334; Abel et al., hep-th/0611130

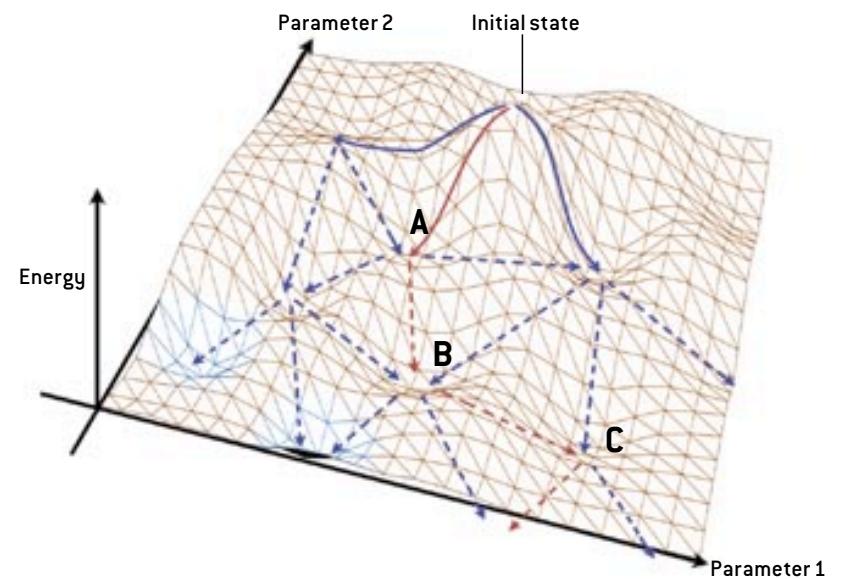
Fischler et al., hep-th/0611018

The Metastable Universe

Metastable vacua appear
to be generic

Arise in embedding
MSSM into string theory

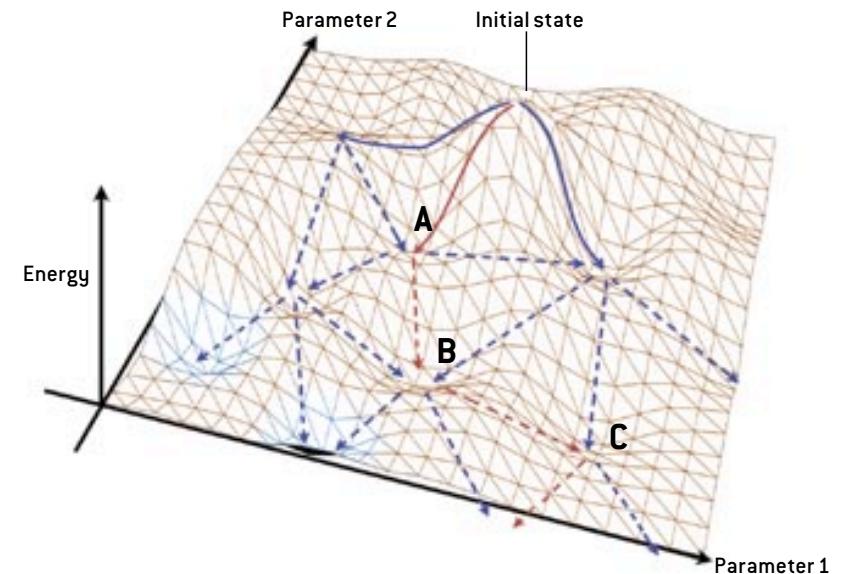
Enjoys the virtues of
DSB (naturalness, etc.)
with fewer constraints
(e.g., Witten index)



The Metastable Universe

An old idea (Dine, Nelson,
Nir, Shirman; Luty &
Terning; Banks;
Dimopoulos, Dvali,
Giudice, Rattazzi)

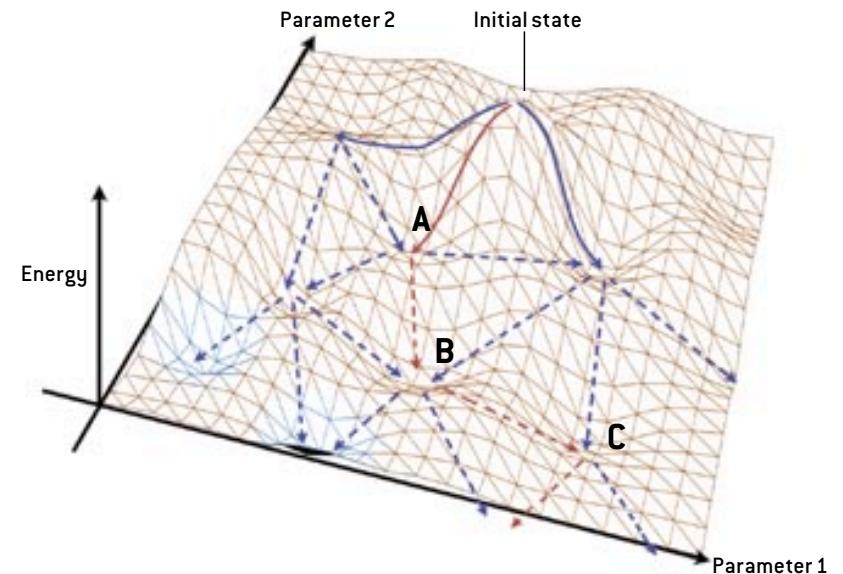
Intriligator, Seiberg, Shih
(ISS) recently found
metastable vacua in SQCD



The Metastable Universe

Validity rests on longevity
of metastable vacua

Useful to ask: how do
theories with metastable
vacua evolve after
reheating?



Metastable SQCD

Intriligator, Seiberg, & Shih uncovered a simple class of metastable SUSY-breaking theories: supersymmetric QCD with fundamental matter

Massive fundamental quarks drive F-term SUSY breaking; dynamical effects restore SUSY at distant vacua

Electric theory

$\mathcal{N} = 1$, $SU(N_c)$ supersymmetric QCD

Fundamental matter Q, Q^c

$$Q \sim (\square_{N_C}, \square_{N_F L}) \quad Q^c \sim (\bar{\square}_{N_C}, \bar{\square}_{N_F R}).$$

$N_C < N_F < \frac{3}{2}N_C$ asymptotically free

Strong coupling scale Λ $m \ll \Lambda$

Superpotential $W_e = m \text{Tr} QQ^c$

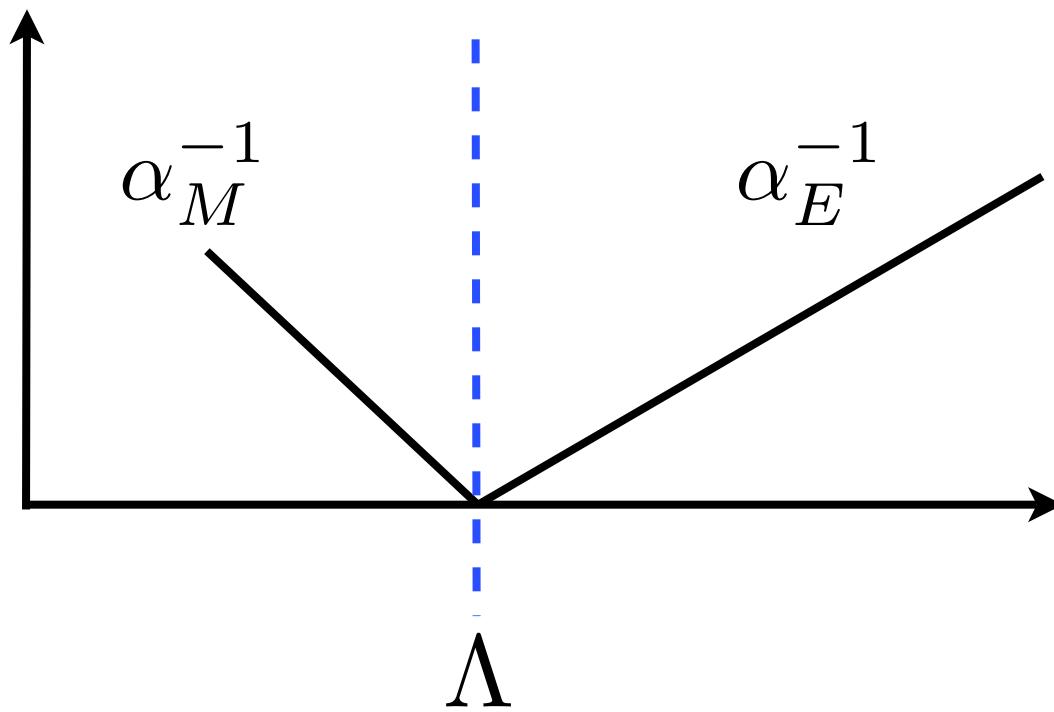
Seiberg duality

Electric theory dual to magnetic gauge
theory w/ $SU(N_F - N_C)$

Magnetic dual is IR free for $N_C < N_F < \frac{3}{2}N_C$

Dual variables are magnetic quarks, meson

Seiberg duality



Magnetic theory

$$SU(N) \qquad N = N_F - N_C \qquad N_F > 3N$$

Magnetic quarks q, q^c , meson $M \sim QQ^c$

$$q \sim (\square_N, \overline{\square}_{N_{F\,L}}) \quad q^c \sim (\overline{\square}_N, \square_{N_{F\,R}}) \quad M \sim (\square_{N_{F\,L}}, \overline{\square}_{N_{F\,R}})$$

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$$W_m = y \operatorname{Tr} q M q^c - \mu^2 \operatorname{Tr} M,$$

Kahler potential smooth near $\mu^2 \sim m\Lambda$
origin, can be taken as canonical

SUSY breaking

$$F_{M_i^j}^\dagger = y\, q_i^a q_a^{c\, j} - \mu^2 \delta_i^j\,,$$

SUSY breaking

$$F_{M_i^j}^\dagger = \boxed{y q_i^a q_a^{c j}} - \boxed{\mu^2 \delta_i^j},$$

↑ ↑
rank $N_F - N_C < N_F$ rank N_F

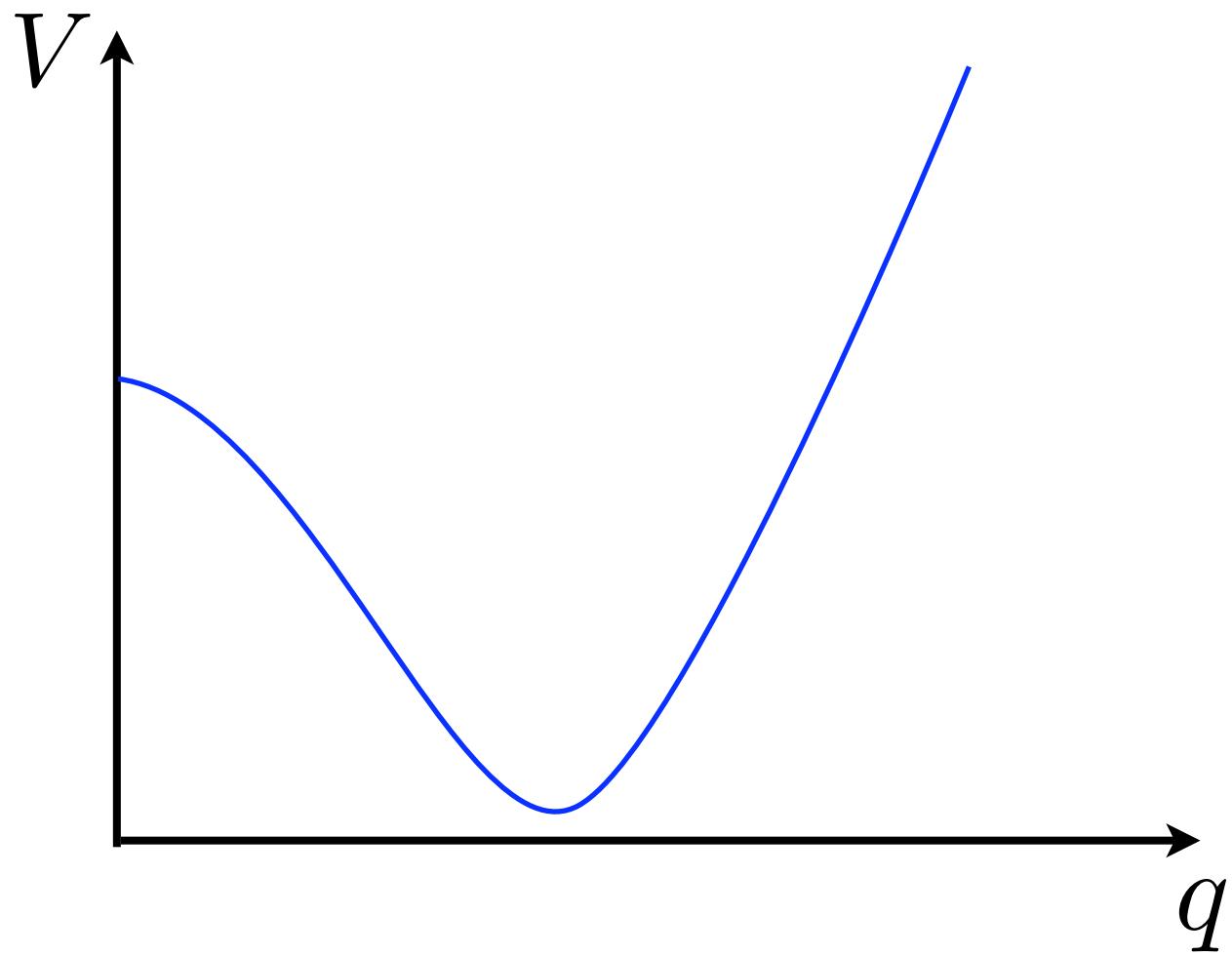
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$$\langle M \rangle_{\text{ssb}} = 0 \quad \quad \langle q \rangle_{\text{ssb}} = \langle q^c \rangle_{\text{ssb}} \sim N \mu \mathbf{1}_N$$

SUSY breaking



SUSY Restoration I

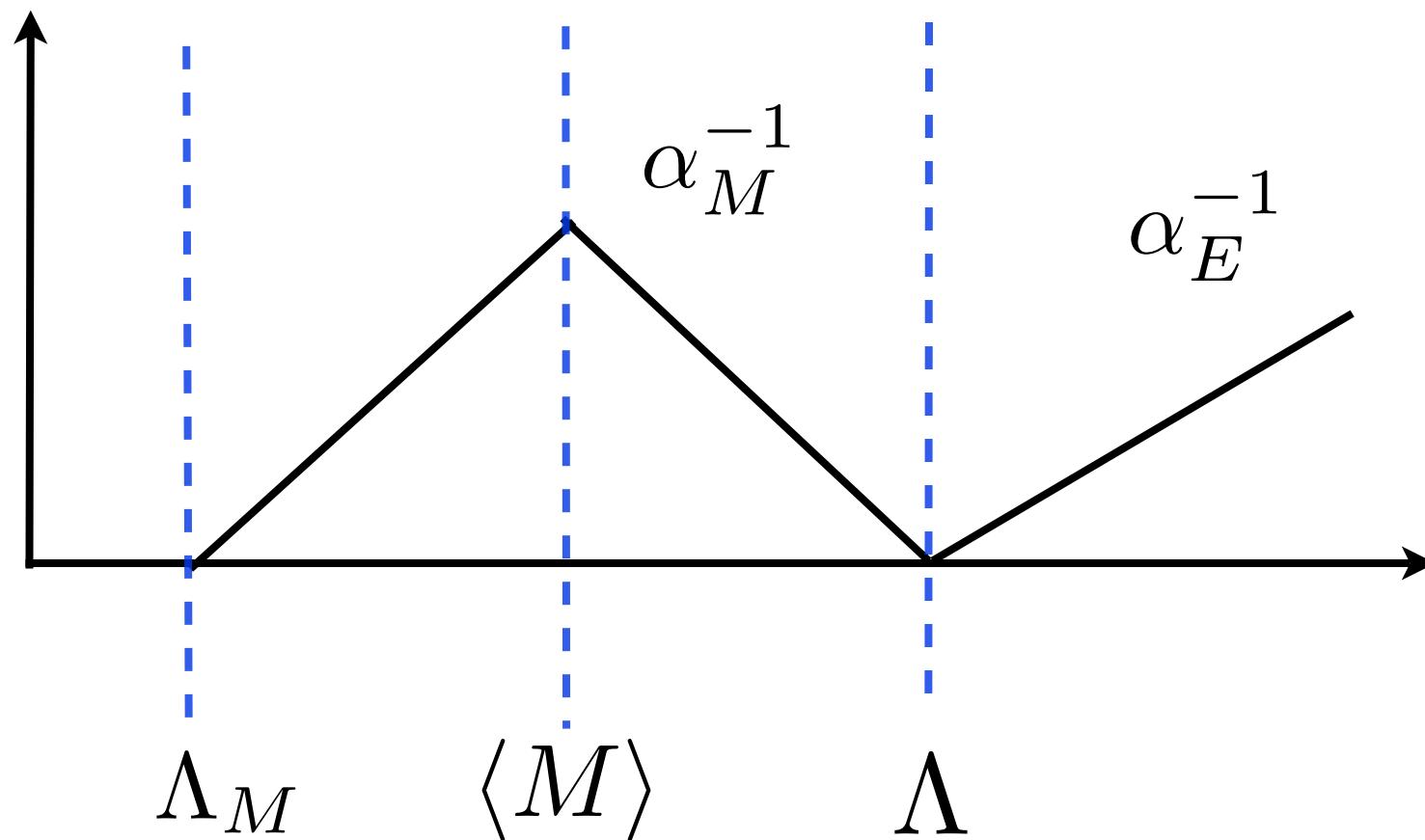
For $\langle M \rangle \neq 0$, magnetic quarks massive;
integrate out $(W_m \supset y \text{Tr} q M q^c)$

Obtain pure SUSY QCD; gaugino
condensation at scale $\Lambda_M \sim M \left(\frac{M}{\Lambda} \right)^{\frac{N_F - 3N}{3N}}$

Generates ADS superpotential

$$W = \left(\frac{\det M}{\Lambda^{N_F - 3N}} \right)^{\frac{1}{N}}$$

SUSY Restoration I



SUSY Restoration II

$$W = -\mu^2 \operatorname{Tr} M + \left(\frac{\det M}{\Lambda^{N_F - 3N}} \right)^{\frac{1}{N}}$$

$$M \sim \eta \mathbb{1} \rightarrow W = -\mu^2 \eta + \eta^{3+a} \Lambda^{-a}$$

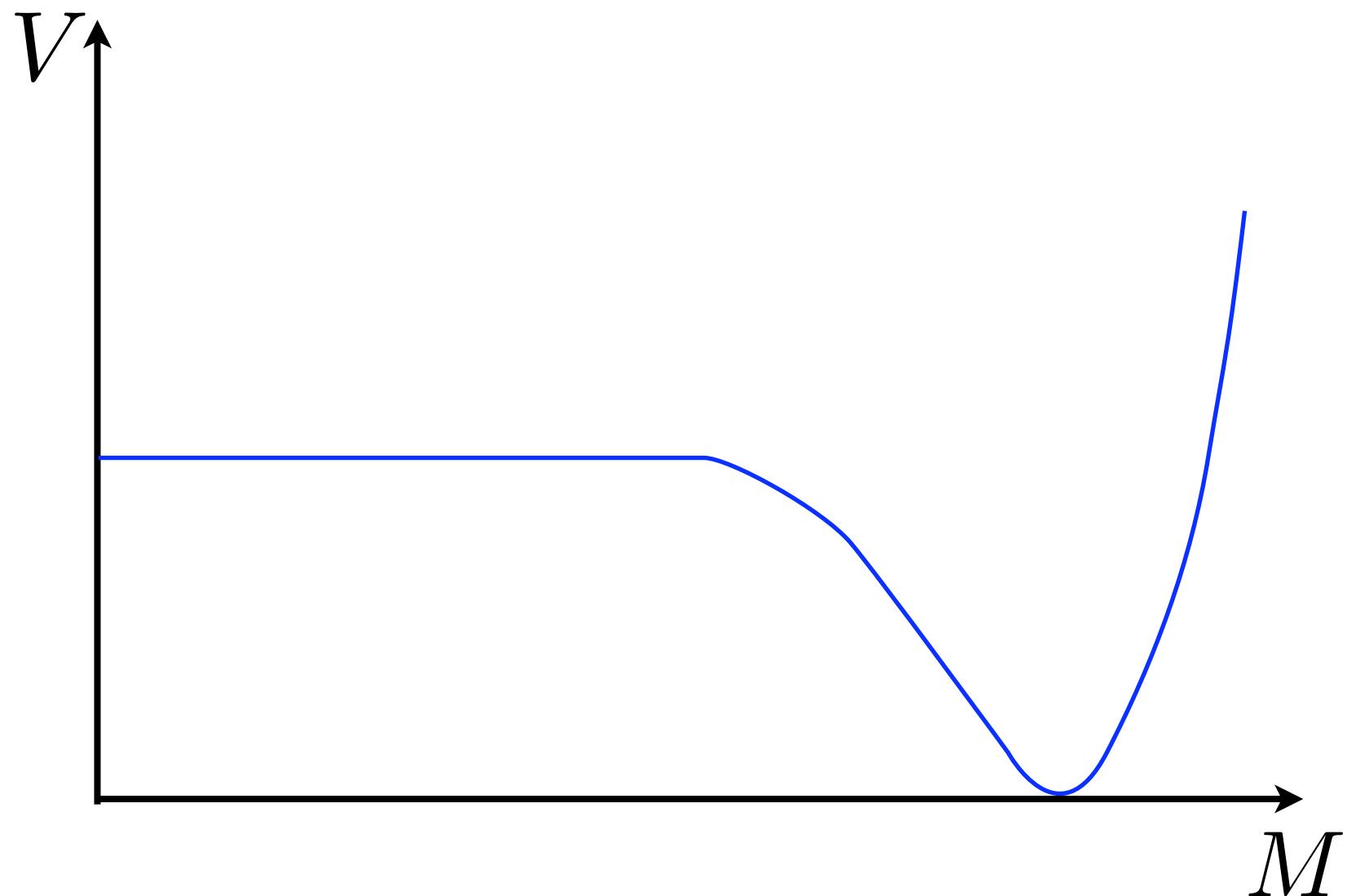
$$a = \frac{N_F - 3N}{N}$$

a parametrizes irrelevance of \det superpotential

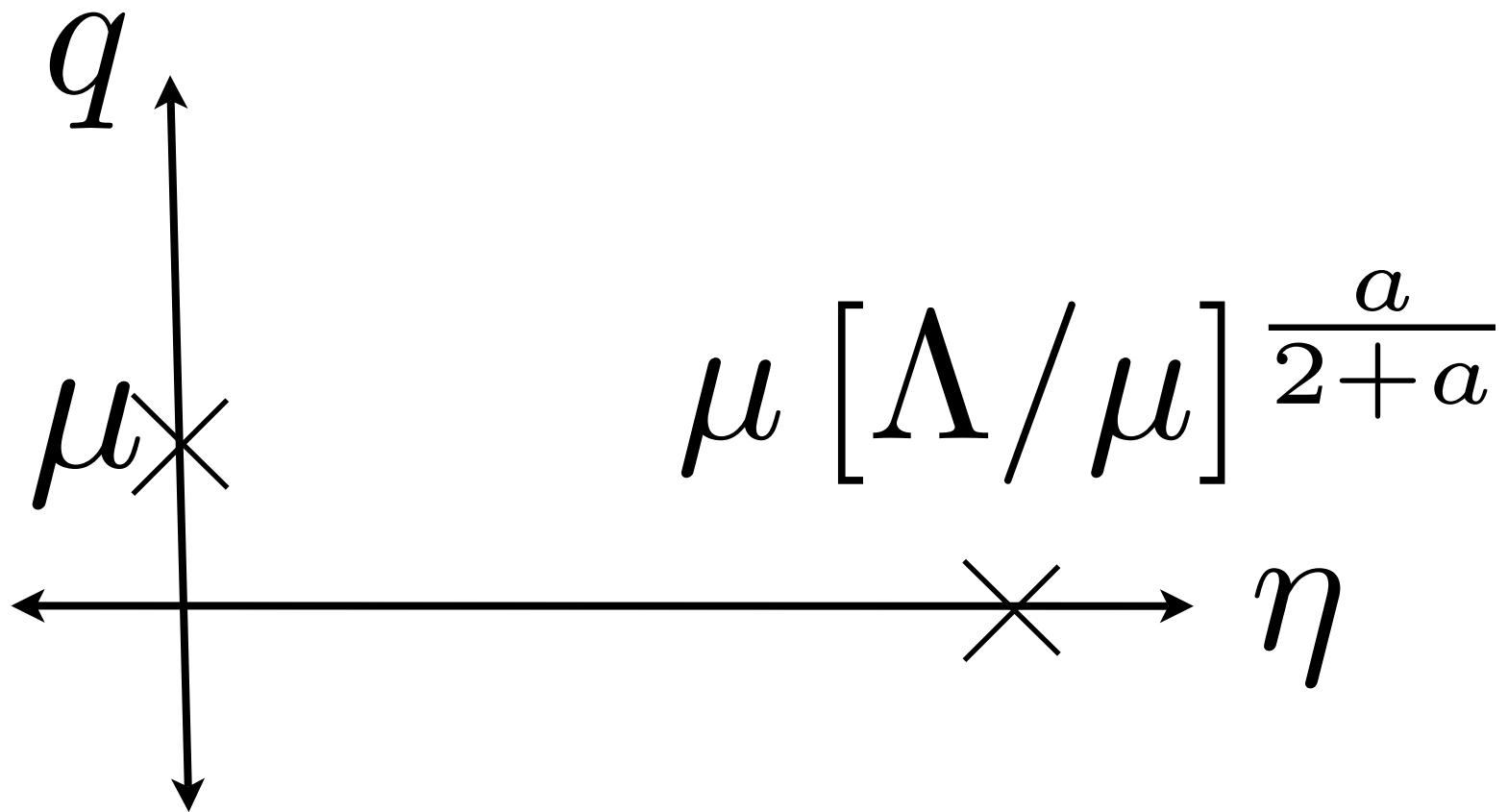
$$F_\eta^\dagger \sim -\mu^2 + \eta^{2+a} \Lambda^{-a} \quad \langle \eta \rangle_{\text{susy}} \sim \mu \left(\frac{\Lambda}{\mu} \right)^{\frac{a}{2+a}}$$

$$V \sim |-\mu^2 + \eta^{2+a} \Lambda^{-a}|^2$$

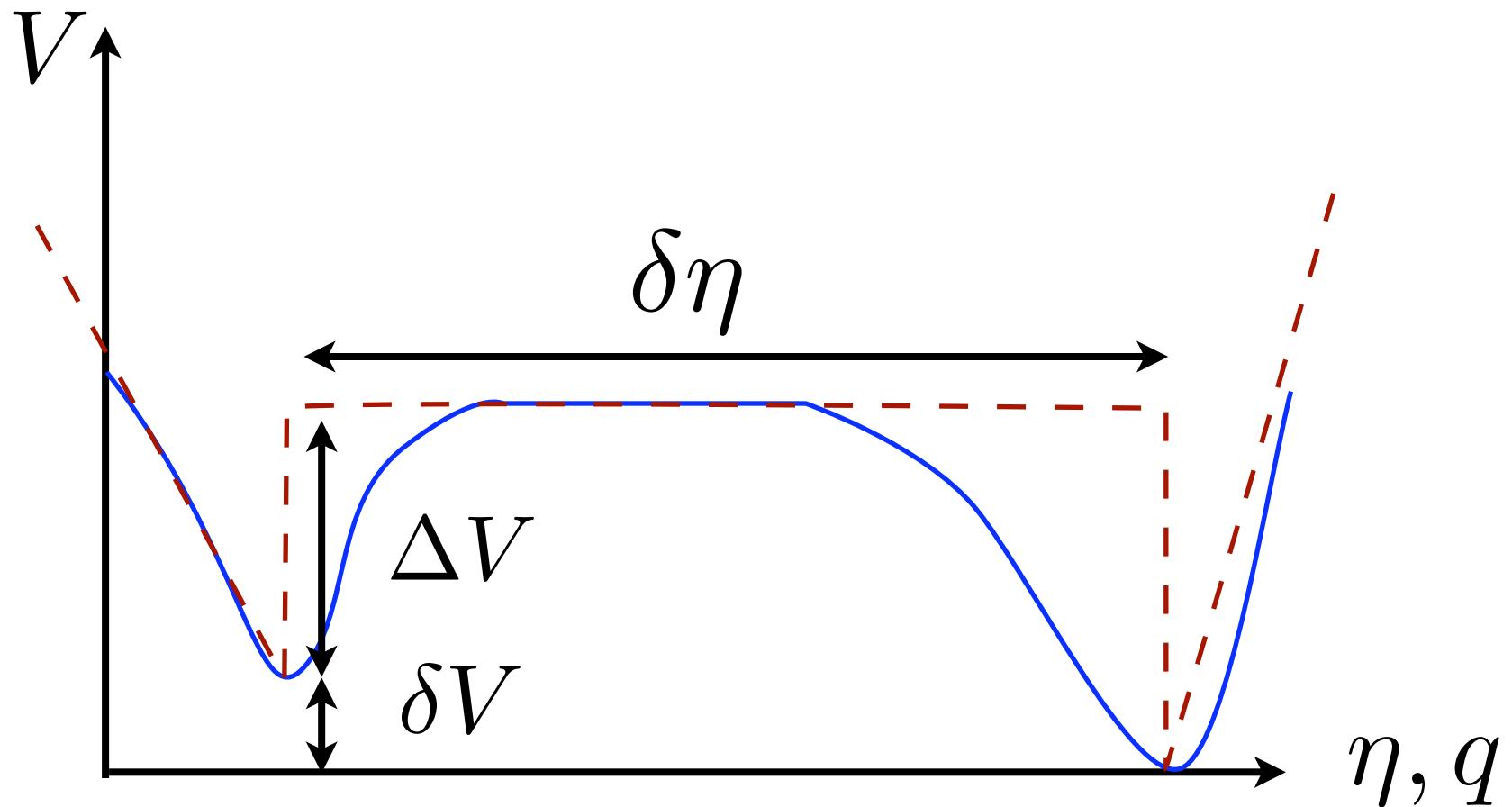
SUSY Restoration II



Metastability



Metastability



$$\Delta V \sim \mu^4$$

$$\delta V \sim \mu^4$$

$$\delta\eta \sim \mu \left(\frac{\Lambda}{\mu}\right)^{\frac{a}{2+a}}$$

Zero-temperature Metastability

Is the metastable vacuum sufficiently long-lived to be phenomenologically viable?

$$\Gamma \sim \mu^4 \exp(-S_4)$$

$$S_4 \sim 2\pi^2 \frac{\Delta\eta_{\text{susy}}^4}{(V_{\text{peak}} - V_{\text{susy}})}$$

$$ISS : S_4 \sim \left(\frac{\Lambda}{\mu}\right)^{\frac{4a}{2+a}}$$

Zero-temperature Metastability

$$\frac{a}{a+2} \log \frac{\Lambda}{\mu} > 0.73 + 0.003 \log \frac{\mu}{\text{Tev}} + 0.25 \log N$$

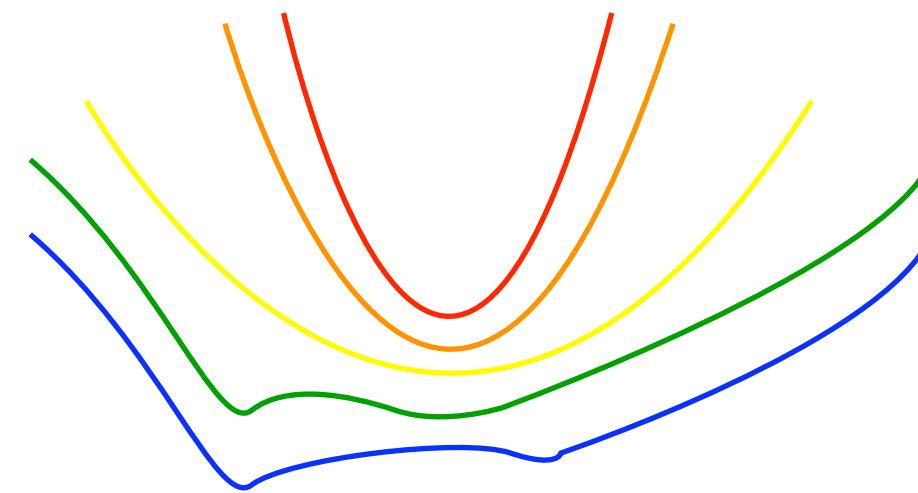
Metastable vacuum is parametrically
long-lived at zero temperature

Reheating SQCD

Natural question: what happens in a finite-temperature universe?

What vacua are selected by cooling?

For temperatures $T \gg \mu$, do thermal effects stimulate transitions?



Thermalization

Analysis assumes hidden sector thermalization, but generically unlikely for the fields to lie in equilibrium configuration after reheating

Difficult to make precise statements (depends on mediation scheme), but some details universal.

Natural to consider regime $\langle Q \rangle \sim H \gg T, \Lambda$ where fluctuations of Q dominate.

Moduli trapping

SQCD electric theory a moduli space in the D-flat directions along which large-vev squarks will oscillate

Origin is an enhanced symmetry point; oscillating squarks dump energy into production of vectors

Moduli trapping

Oscillations damp rapidly in a time $t_{\text{damp}} \sim \frac{2\pi}{m} \left(\frac{2\pi}{g}\right)^{3/2}$

Electric quarks localize at origin; thermal equilibrium reached at $T \gg \mu$

Similar analysis goes through for $\Lambda > \langle Q \rangle > T$

Thermal effective potential

Compactify Euclidean time with radius $R_\tau \sim T^{-1}$
to obtain finite-temperature 2-point function

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to obtain finite-temperature 2-point function

$$\begin{aligned}\delta V(\phi, T) = & \sum_{\alpha, \text{boson}} \left(-\frac{\pi^2}{90} T^4 + \frac{1}{24} m_\alpha^2(\phi) T^2 + \dots \right) \\ & + \sum_{\alpha, \text{fermion}} \left(-\frac{7}{8} \frac{\pi^2}{90} T^4 + \frac{1}{48} m_\alpha^2(\phi) T^2 + \dots \right)\end{aligned}$$

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↑
added entropy for light species

Thermal effective potential

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Early Universe

At high temperatures, fields lie at minimum of free energy; for $T \gg \mu$ this is $\langle q \rangle, \langle M \rangle = 0$

Point of maximum symmetry

Early Universe

As temperature drops, two possible phase transitions:

1. To metastable vacuum, $\langle q \rangle \neq 0$
2. To the SUSY vacuum $\langle M \rangle \neq 0$

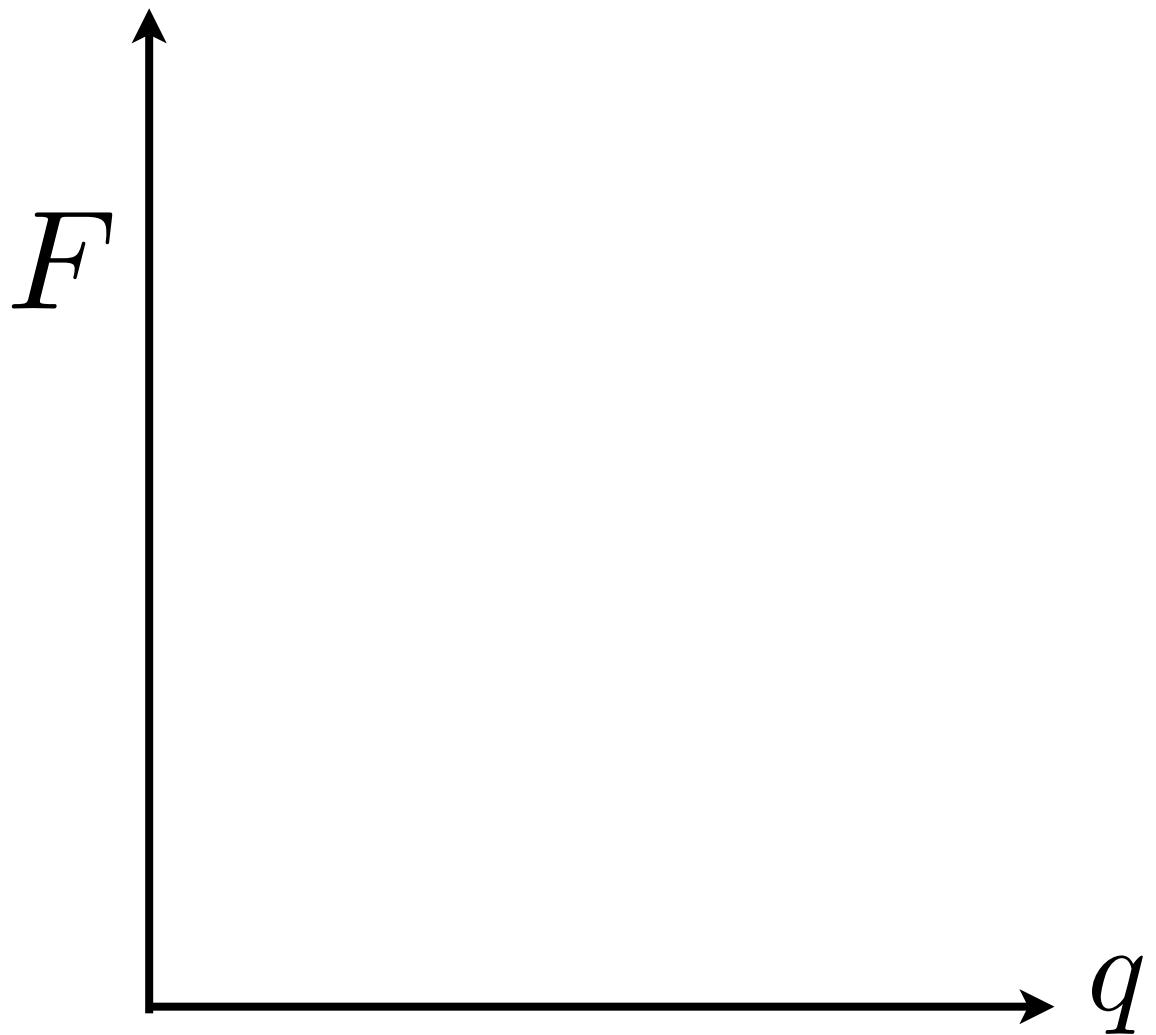
Which transition dominates depends on critical temperature, order of transitions.

Transition to the metastable vacuum

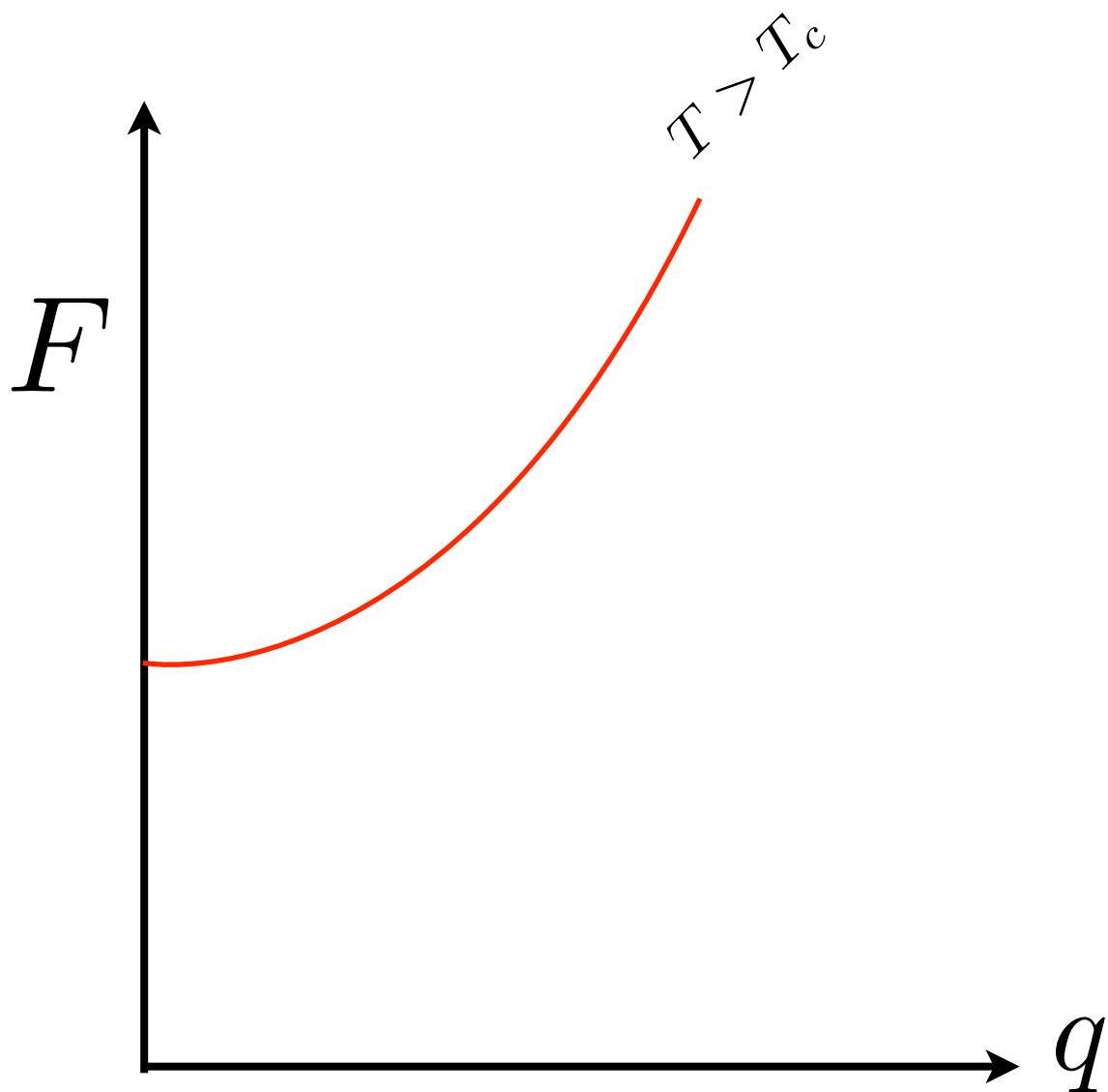
$$F = N \left(\frac{yq^2}{N^2} - \mu^2 \right)^2 - c_0 N_F^2 T^4 + (c_1^{(g)} g^2 + c_1^{(y)} y^2) N q^2 T^2 + \dots$$
$$\sim (-y\mu^2 + y^2 T^2) q^2 + \dots$$

Second-order transition at $T_{c,ssb} \simeq \mu$

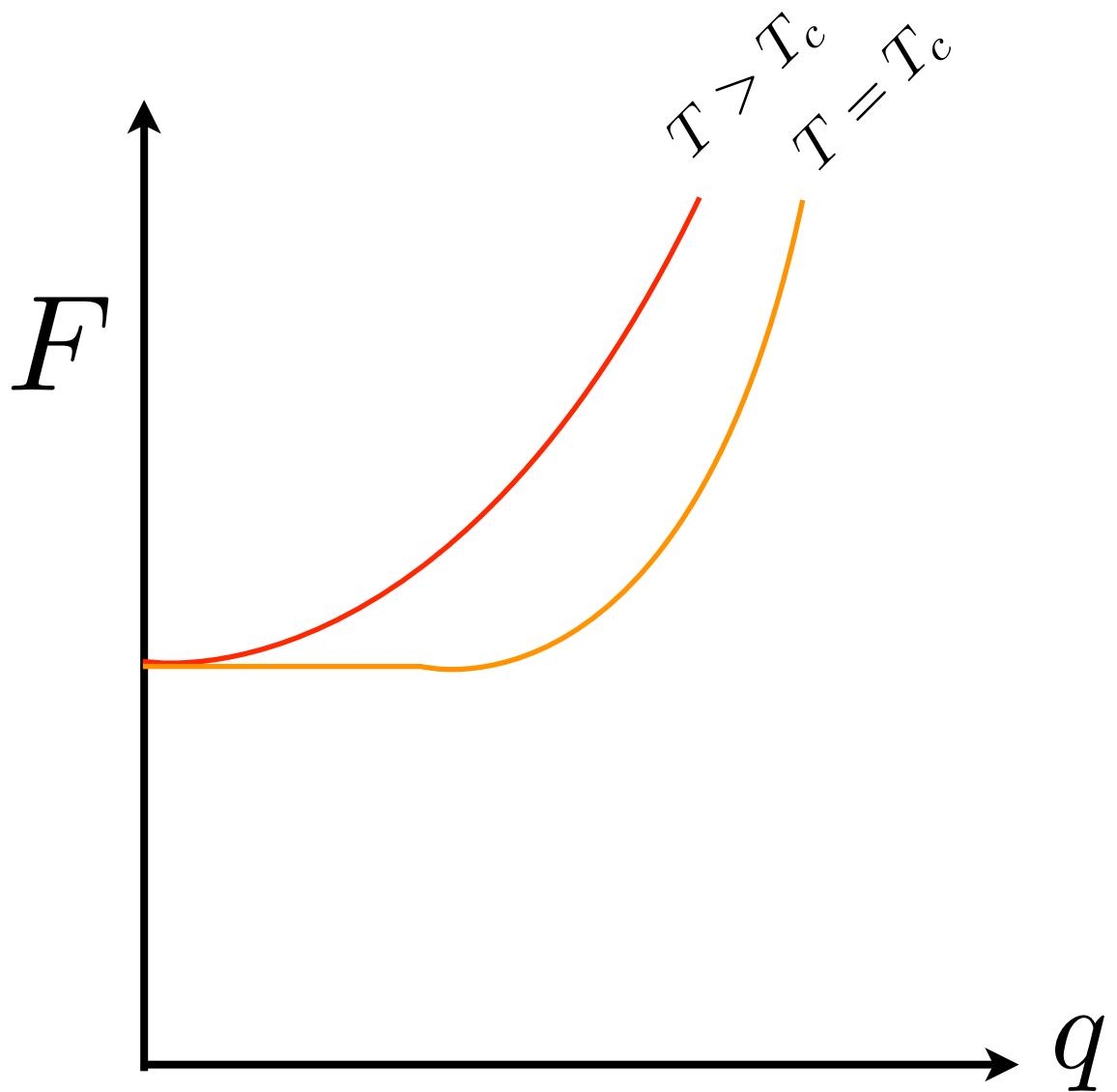
Transition to the metastable vacuum



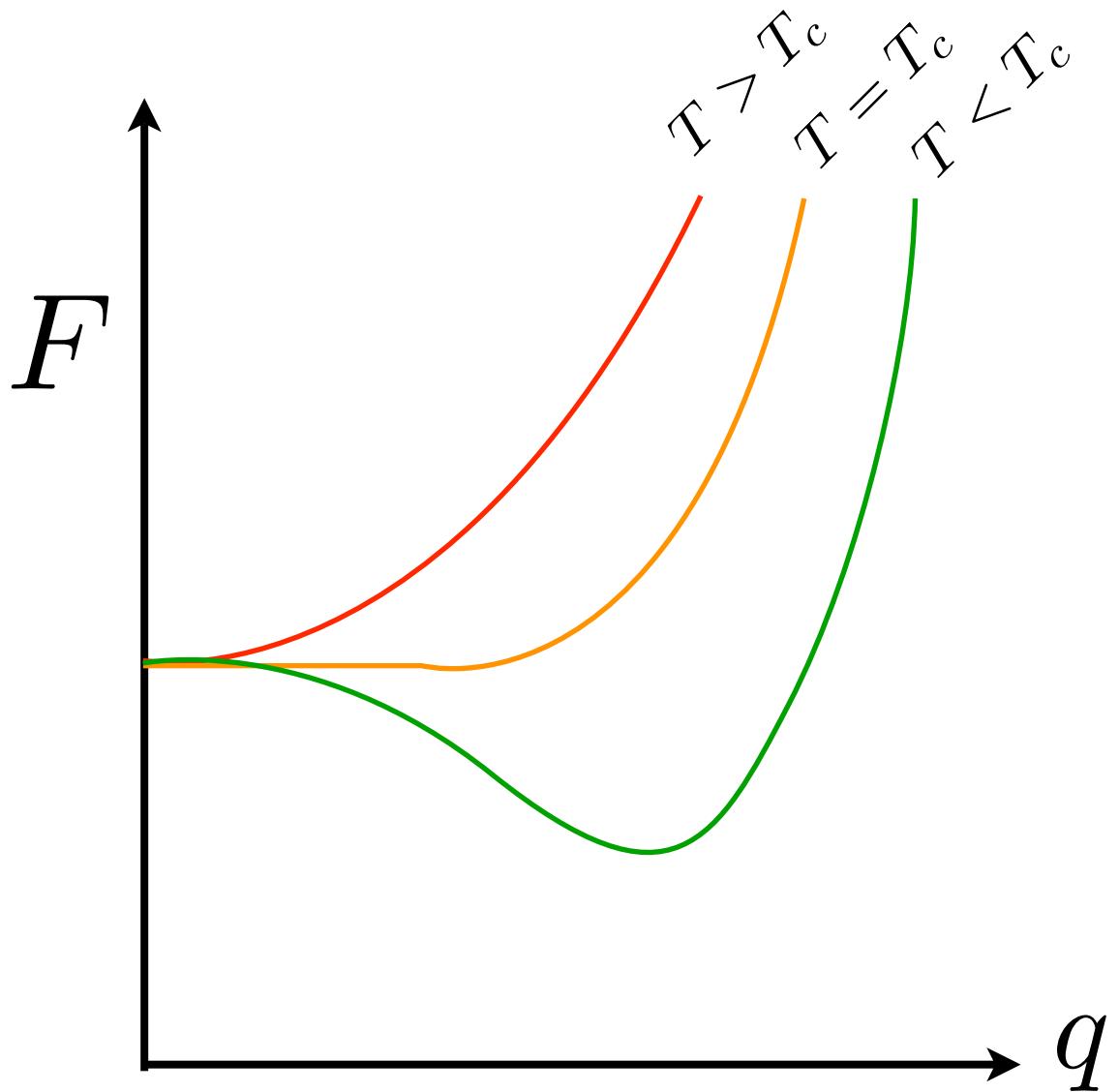
Transition to the metastable vacuum



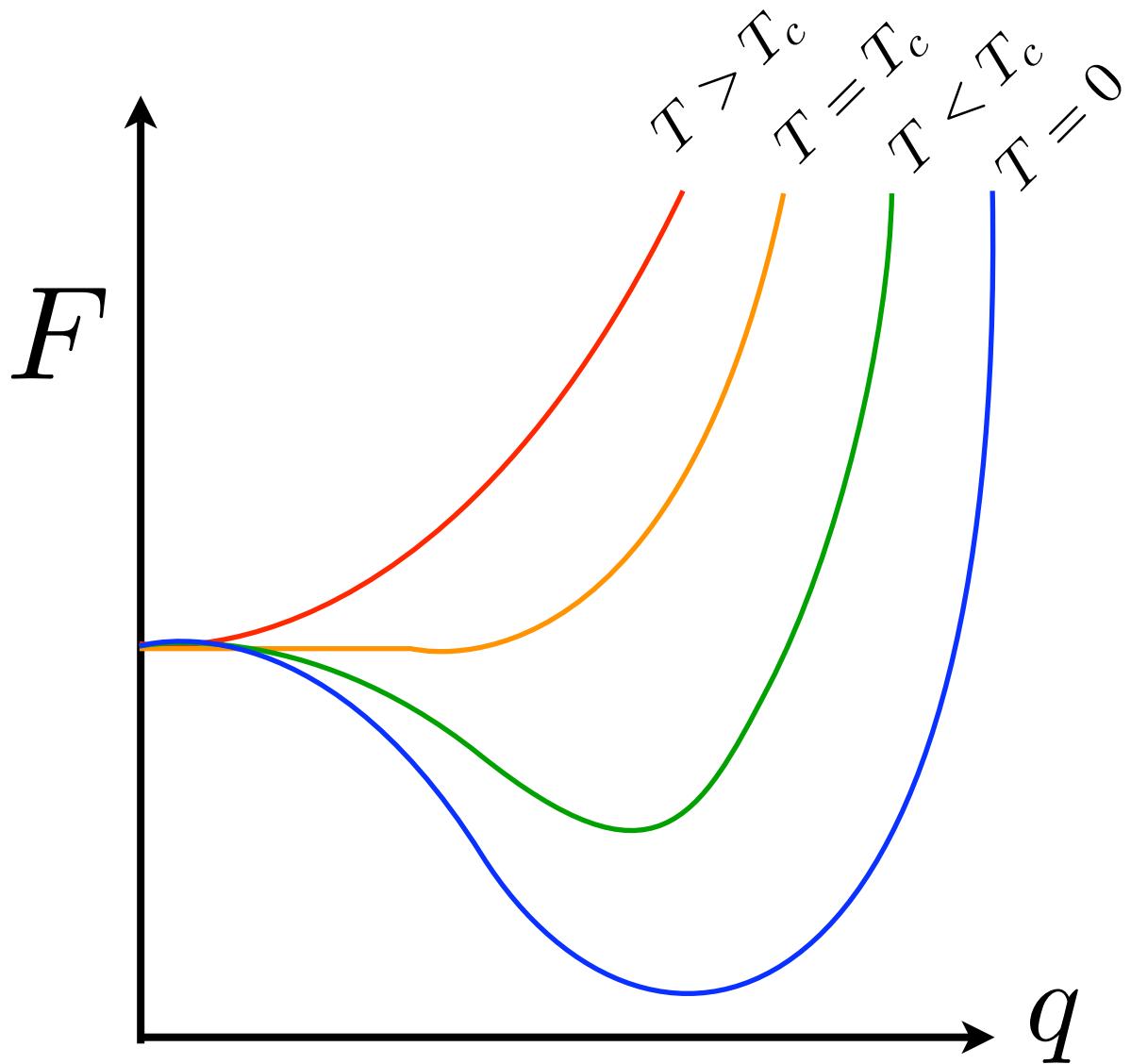
Transition to the metastable vacuum



Transition to the metastable vacuum



Transition to the metastable vacuum



Transition to SUSY vacuum I

$$V = \begin{cases} \mu^4 + c_1 y^2 N \eta^2 T^2 - c_0 (N N_F + N^2) T^4 + \dots & T \geq \Lambda_m(\eta) \\ N \Lambda^4 \left| \left(\frac{\eta}{\sqrt{N_F} \Lambda} \right)^{2+a} - \frac{\mu^2}{\Lambda^2} \right|^2 \\ \quad + c_1 y^2 N \eta^2 T^2 - c_0 (N N_F + N^2) T^4 + \dots & T \geq y\eta \\ N \Lambda^4 \left| \left(\frac{\eta}{\sqrt{N_F} \Lambda} \right)^{2+a} - \frac{\mu^2}{\Lambda^2} \right|^2 & T < y\eta \end{cases}$$

Near origin, $\sim y^2 \eta^2 T^2 - \mu^2 \Lambda^{-a} \eta^{2+a}$
 → quarks stabilize origin even at low temp

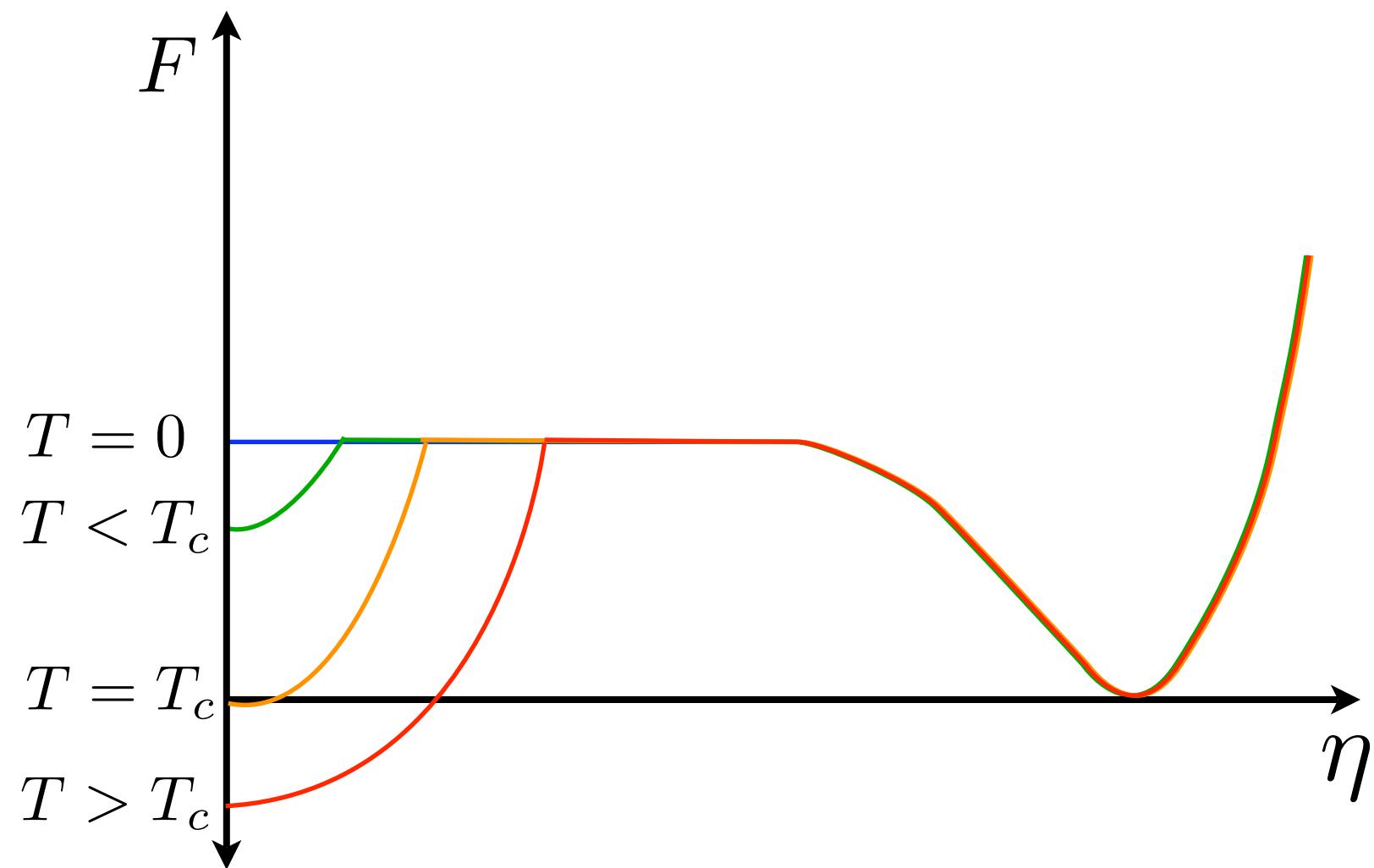
First-order transition at $T_{c,susy} \sim \mu$

Transition to SUSY vacuum I

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Transition temperatures into
SUSY, metastable vacua are
parametrically the same

Transition to SUSY vacuum I



Transition to SUSY vacuum: Bubble nucleation

$$\Gamma \sim T^4 e^{-S_3/T}$$

$$S_3 \sim \frac{4\pi}{3\sqrt{2}} \frac{\Delta\eta_{\text{susy}}^3}{\left[(V_{\text{peak}} - V_{\text{susy}})^{\frac{1}{4}} - (V_{\text{peak}} - V_0)^{\frac{1}{4}} \right]^2}$$

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$$R_c \sim \frac{\Delta\eta_{\text{susy}} \Delta V^{\frac{1}{2}}}{\delta V} \quad \begin{aligned} \Delta V &\simeq \mu^4 \\ \delta V &\simeq \mu^4 \left(1 - \left(\frac{T}{T_c^{\text{susy}}} \right)^4 \right) \end{aligned}$$

Finite-temp longevity bound

$$\log \frac{\Gamma}{\mu^4} \simeq -\frac{9\pi}{\sqrt{2N}} \left(\frac{\Lambda}{\mu}\right)^{\frac{3a}{2+a}}.$$

$$\Gamma(T)\,a^3(T)\,\mathcal{V}\Delta t\simeq 0$$

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same parametric
dependence

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size of universe when
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size of universe when
bubble was active

$$\Gamma(T) a^3(T) \mathcal{V} \Delta t \simeq 0$$

duration of thermal
tunneling epoch

same parametric
dependence

Finite-temp longevity bound

$$\frac{a}{a+2} \log \frac{\Lambda}{\mu} > 0.64 - 0.010 \log \frac{\mu}{\text{Tev}} + 0.17 \log N$$

Same parameter ensuring the longevity of the metastable vacuum also favors its selection during thermal evolution

Morals

Rule of thumb for evolution of theories
with metastable SUSY-breaking vacua?

The universe cools to the vacuum with the
greater abundance of light states.

Favorable outcome for SQCD (and
variations thereof, e.g., SQCD with
adjoints)

Outlook & Future directions

- Metastable DSB for direct gauge mediation
(Dine & Mason; Kitano, Ooguri, &
Ookouchi; Aharony & Seiberg; Murayama
& Nomura; Csaki, Shirman, & Terning)
- Metastable SUSY breaking in string vacua
(vast & ever-growing literature...)
- Inflation into the metastable vacuum?