

# Quantum field theory for correlated many-body systems

- Introduction to correlated many-body systems
- Second Quantization
- One- and two-particle Green's functions, Matsubara Formalism
- Diagrammatic perturbation theory and Feynman diagrams
- (Fermi liquid theory)
- Linear response theory
- Applications: Magnetism and (Super)conductivity
- Outlook: Dynamical mean field theory and beyond

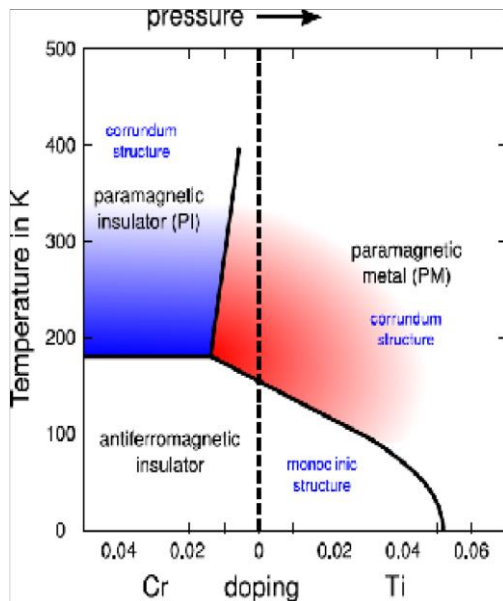
## Literature

- A. A. Abrikosov, L. P. Gorkov, I. E. Dzyaloshinski, Methods of Quantum Field Theory in Statistical Physics, Dover Publications, Inc. New York, 1963
- A. Altland and B. Simons, Condensed Matter Field Theory, Cambridge University Press, 2010.
- K. Elk und W. Gasser, Die Methode der Greenschen Funktionen in der Festkörperphysik, Akademie Verlag, Berlin 1979
- A. L. Fetter and J. D. Walecka, Quantum Theory of Many-Particle Systems, Dover Publications, 2003.
- A. M. Zagoskin, Quantum Theory of Many-Body Systems, Springer Science+Business Media New York, 1998.

# Why are correlated many-body (many-electron) systems interesting?

- Interesting physical phenomena
- Potentially of technological relevance

## Mott-metal-insulator transition in $V_2O_3$

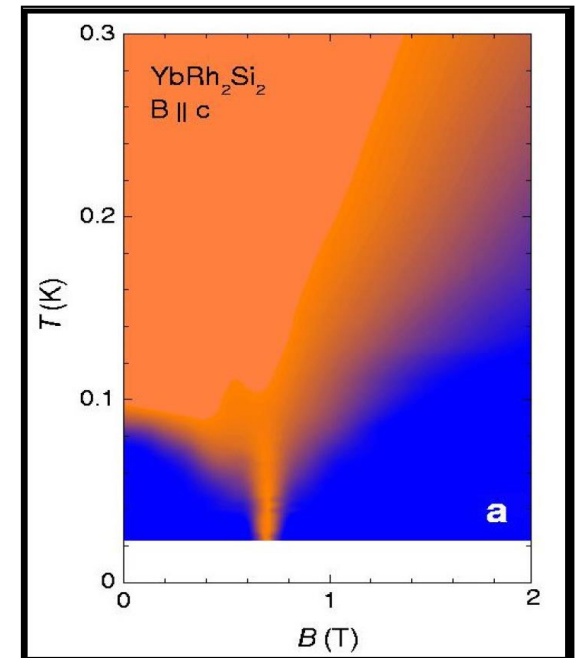


Mc Whan et al., PRB (1973)

## High-temperature superconductivity

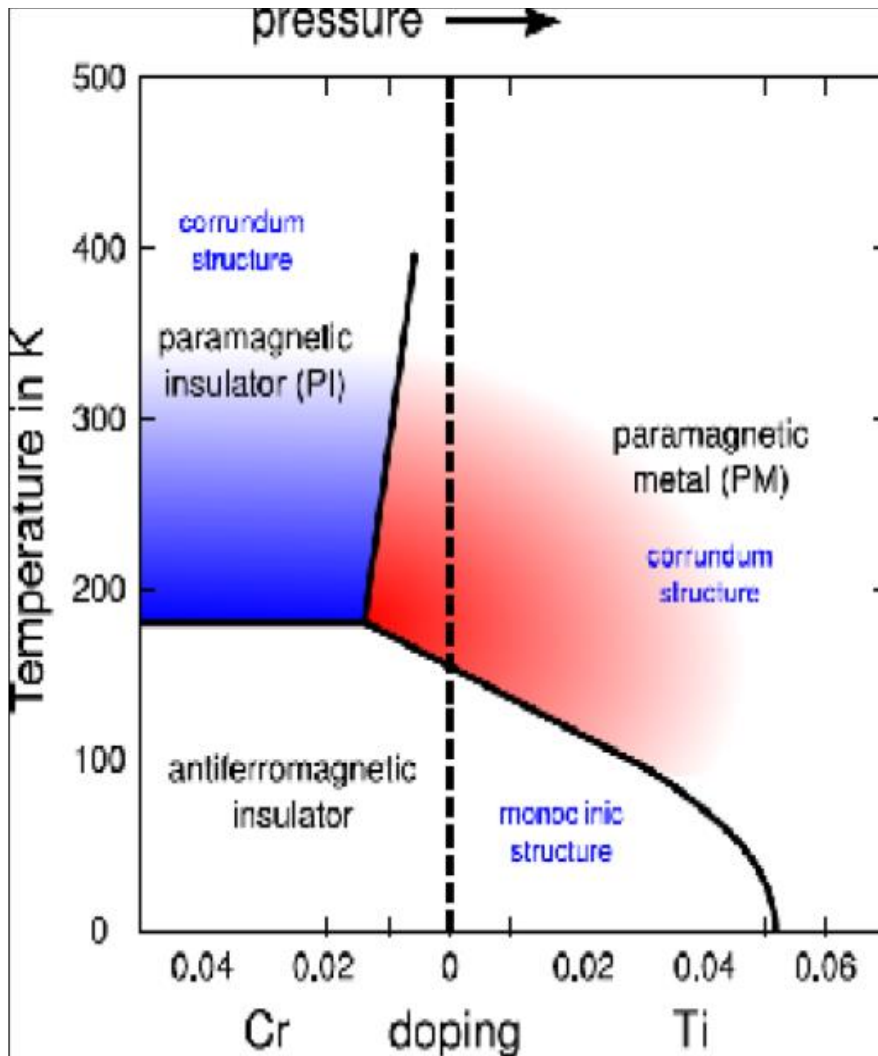


## Quantum critical points



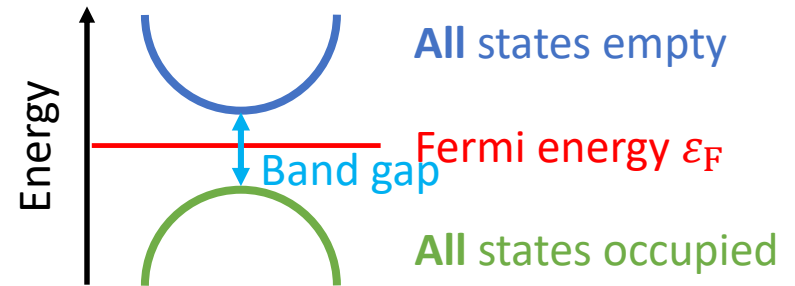
J. Custer et al., Nature (2003)

## Mott-metal-insulator transition in $V_2O_3$



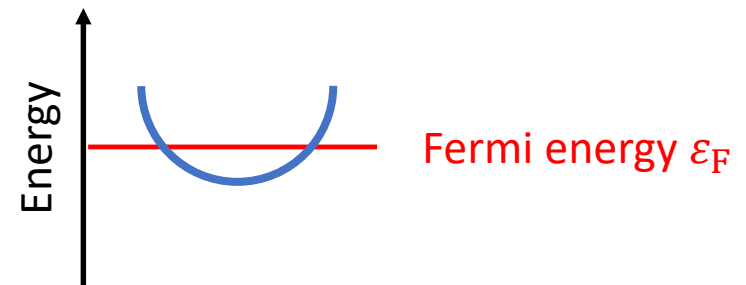
Mc Whan et al., PRB (1973)

### „Normal“ Band insulator



⇒ No electrons available for conduction

### Here: Correlation-driven insulator



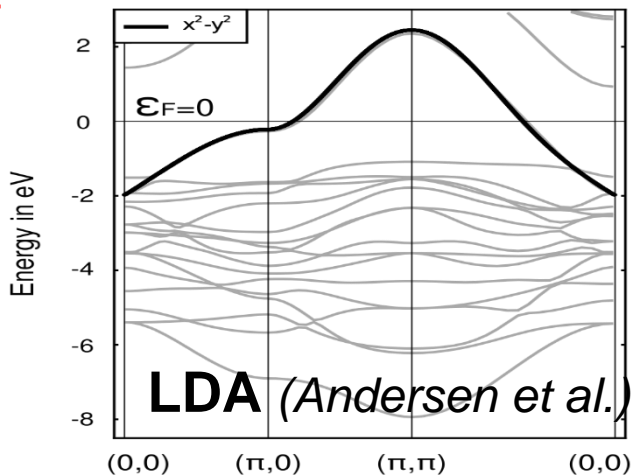
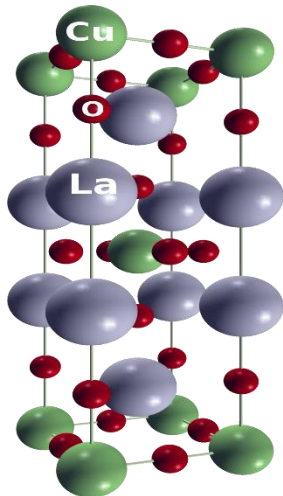
⇒ Band crosses the Fermi level:  
electrons are available for conduction

⇒ Insulator due to Coulomb repulsion  
between the electrons!

# High-temperature superconductivity – The Cuprates



e.g.:  $\text{La}_2\text{CuO}_4$



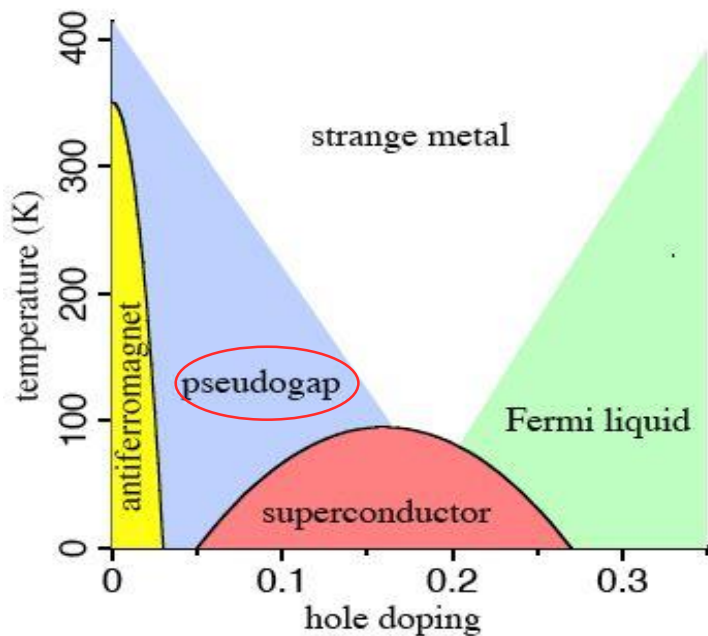
- $\text{CuO}_2$  planes
- La,O layers

$\text{Cu}^{2+}$  (Ar  $3d^9$ )

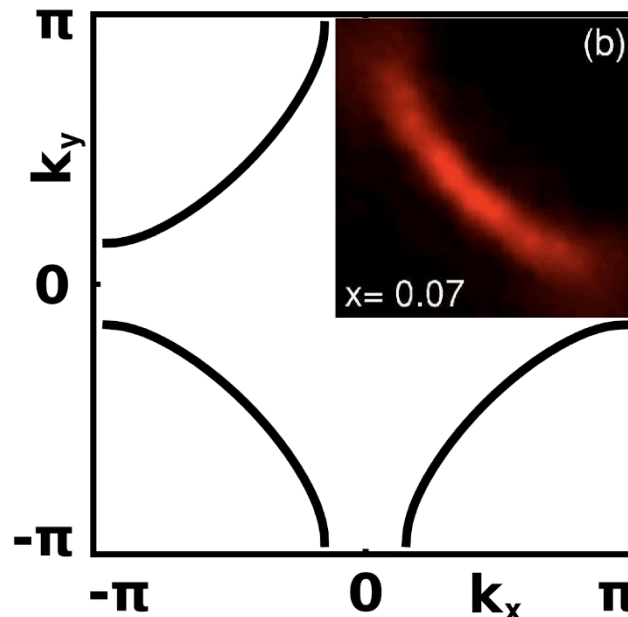
$\text{O}^{2-}$  (He  $2s^2 2p^6$ )

hole doping:

$\text{La}^{3+} \rightarrow \text{Sr}^{2+}$



ARPES:



Yoshida et al., PRB 74, 224510 (2006).