

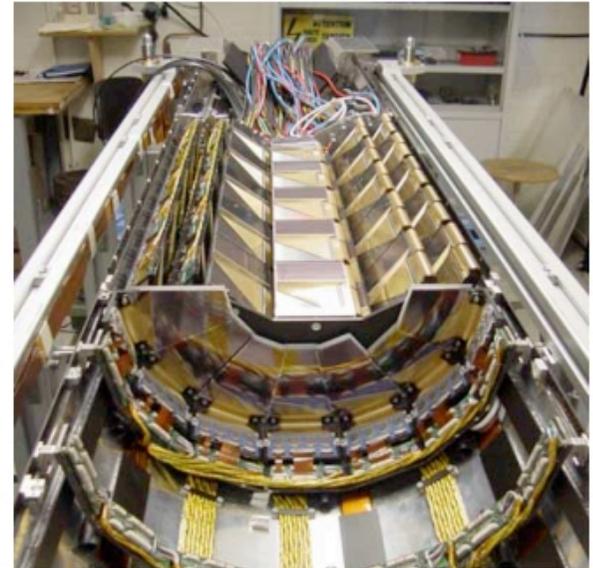
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# Semiconductor-Detectors

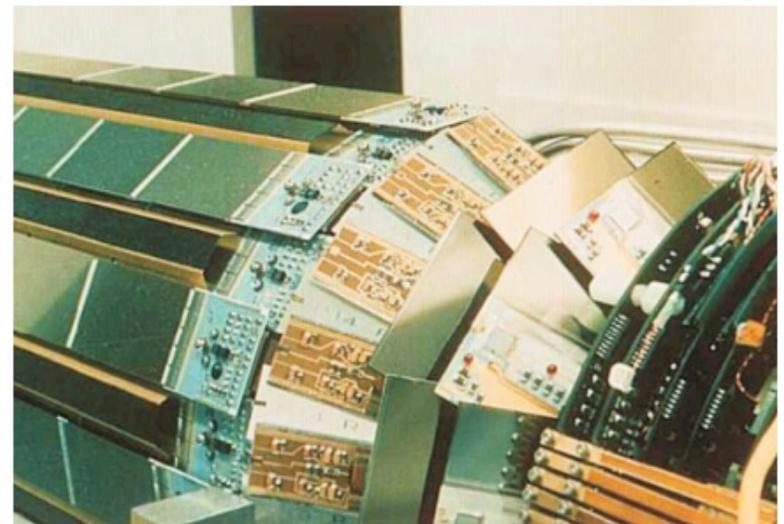


# Motivation

- ~ 1950: Discovery that pn-- junctions can be used to detect particles.
- Semiconductor detectors used for energy measurements ( Germanium)
- Since ~ 30 years: Semiconductor detectors for precise position measurements.
- precise position measurements possible through fine segmentation ( 10-- 100 $\mu\text{m}$ )
- multiplicities can be kept small (goal:<1%)
- Technological advancements in production technology
- developments for micro electronics



ZEUS MVD 2000



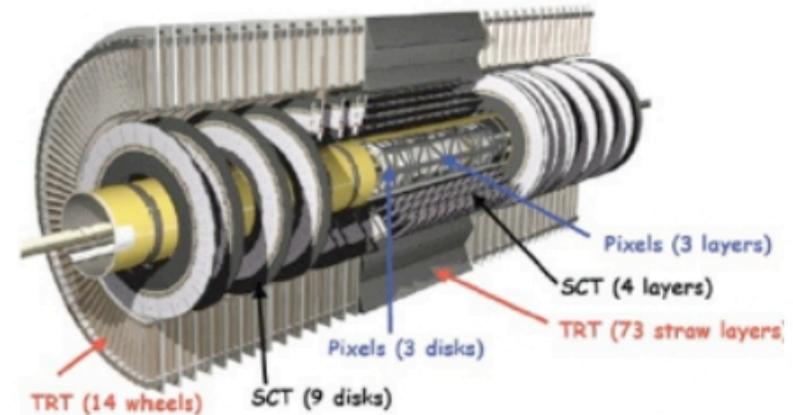
DELPHI VFT 1996

# Large Silicon Systems

## ATLAS

Strips: 61 m<sup>2</sup> of silicon, 4088 modules, 6x10<sup>6</sup> channels

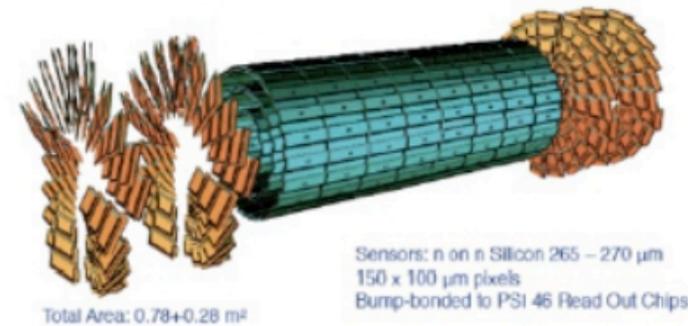
Pixels: 1744 modules, 80 x 10<sup>6</sup> channels



## CMS

the world largest silicon tracker  
200 m<sup>2</sup> of strip sensors (single sided)  
11 x 10<sup>6</sup> readout channels

~1m<sup>2</sup> of pixel sensors, 60x10<sup>6</sup> channels

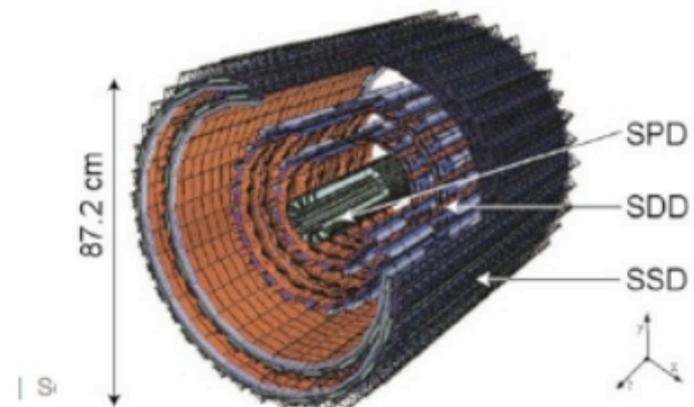


## ALICE

Pixel sensors  
Drift detectors  
Double sided strip detectors

## LHCb

VELO: Si Strips

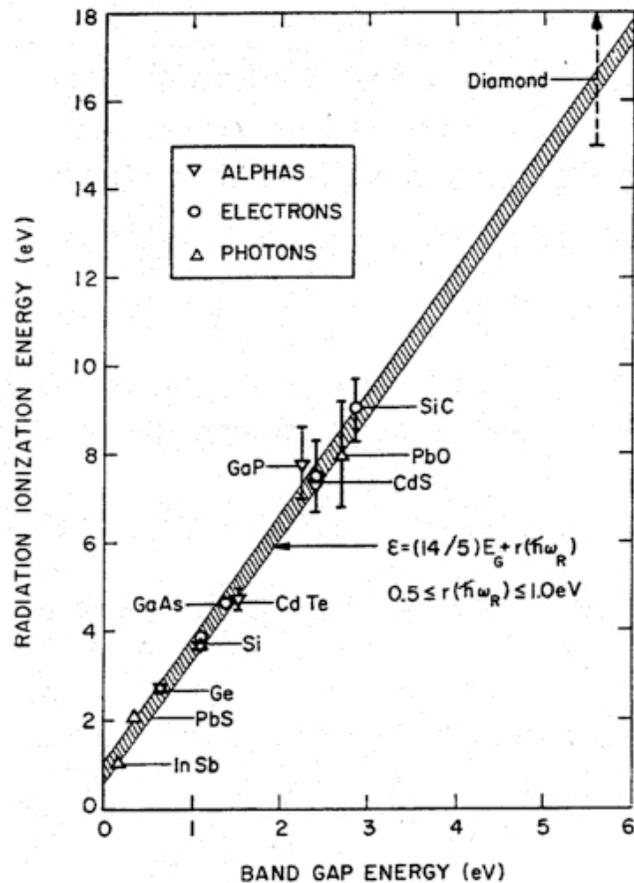
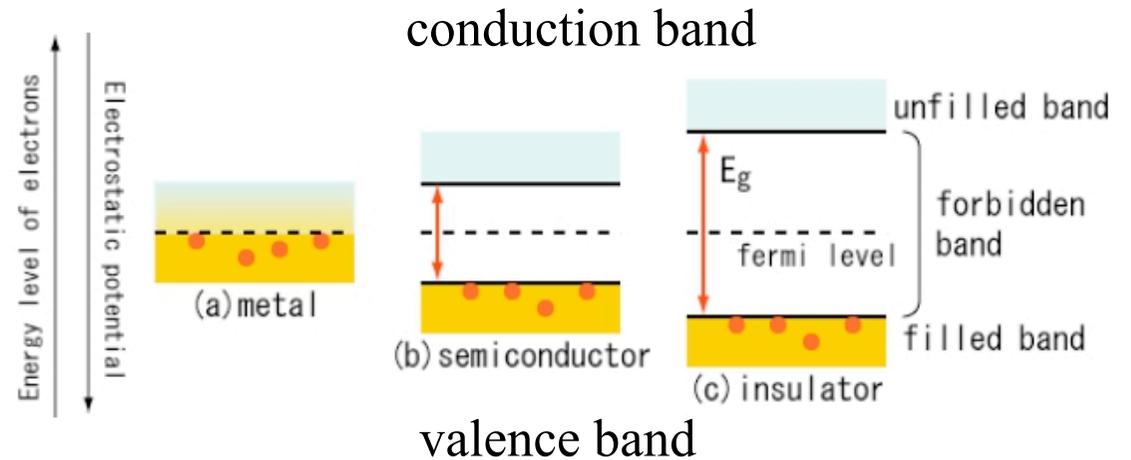


# Pros/Cons of semiconductors as detection material

- Semiconductor detectors have a **high density**
- Large energy loss over short distance: thin detectors
- Diffusion effect is smaller than in gas detectors resulting in achievable position resolution of less than 10  $\mu\text{m}$
- **Low ionization energy** (few eV per e - hole pair) compared to gas detectors (20 - 40 eV per e - ion pair) or scintillators (400 - 1000 eV to create a photon)
- Typically no internal amplification, i.e. small signal with a few exceptions (getting more common)
- High cost per surface unit
  - silicon, read out chips, cooling
  - High number of readout channels
  - Large power consumption → cooling

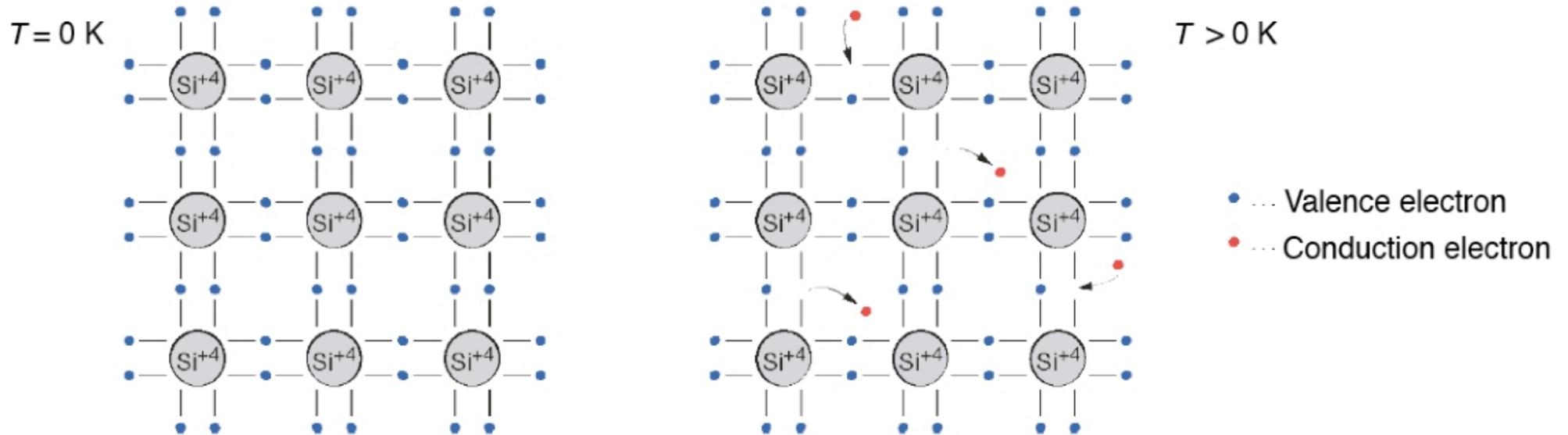
# Energy bands

- In free atoms the electron energy levels are discrete.
- In a solid, energy levels split and form nearly - continuous bands



- Large gap: the solid is an insulator
- No gap: it is a conductor
- Small band gap: **semiconductor**
- For silicon, the band gap is 1.12 eV, but it takes 3.6 eV to ionize an atom   
 → rest of the energy goes to phonon excitations (heat).

# Band Model for Elements IV (Example for Si)



Each atom has 4 closest neighbors, the 4 electrons in the outer shell are shared and form covalent bonds.

- At low temperature all electrons are bound
- At higher temperature, thermal vibrations break some of the bonds
- free e- cause conductivity (electron conduction)
- The remaining open bonds attract other e- → the “holes” change position (hole conduction)

# Intrinsic Carrier Concentration

- Due to the small band gap in semiconductors, electrons already occupy the conduction band at room temperature.
- Electrons from the conduction band may recombine with holes.
- A **thermal equilibrium** is reached between **excitation** and **recombination** : charge carrier concentration  $n_e = n_h = n_i$

intrinsic carrier concentration:

$$n_i = \sqrt{N_C N_V} \cdot \exp\left(-\frac{E_g}{2kT}\right) \propto T^{\frac{3}{2}} \cdot \exp\left(-\frac{E_g}{2kT}\right)$$

factor 2  
every  $\Delta T$   
= 8°K

- In ultra- pure silicon the intrinsic carrier concentration is  $1.45 \cdot 10^{10} \text{ cm}^{-3}$  .
- With approximately  $10^{22} \text{ Atoms/cm}^3$  about 1 in  $10^{12}$  silicon atoms is ionized

(Ge:  $n_i = 2.4 \cdot 10^{13} \text{ cm}^{-3}$  at 300K)

(\*)  $N_C$  and  $N_V$  are the density of states in the valence and conduction band, respectively

# Elemental Semiconductors

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**Germanium:** Needs cooling due to small band gap of 0.66 eV ( liquid N<sup>2</sup> at 77 K)  
mainly used in nuclear physics: Very good energy resolution!

**Silicon:** Can be operated at room temperature (band gap of 1.12 eV)  
Synergies with micro electronics industry  
Standard material for detectors in high energy physics

**Diamond** ( CVD \* or single crystal): Allotrope of carbon  
Large band gap of 5.5 eV (requires no depletion zone)  
Very radiation hard  
Disadvantages: low signal and high cost

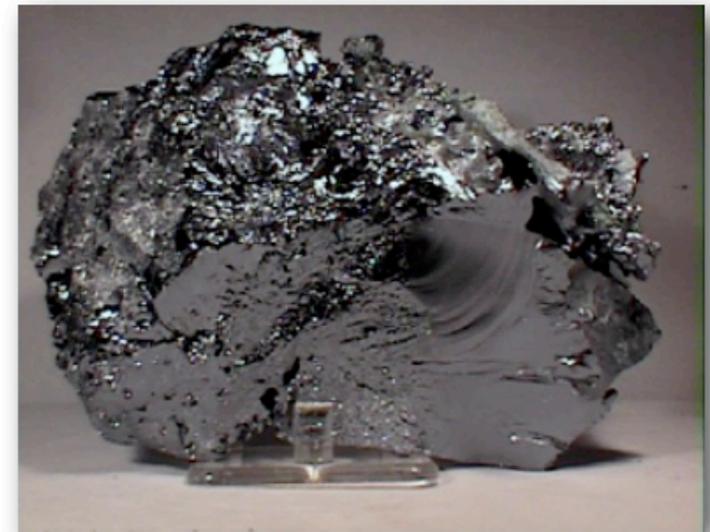
(\* ) CVD: Chemical Vapor Deposition

# Material Properties

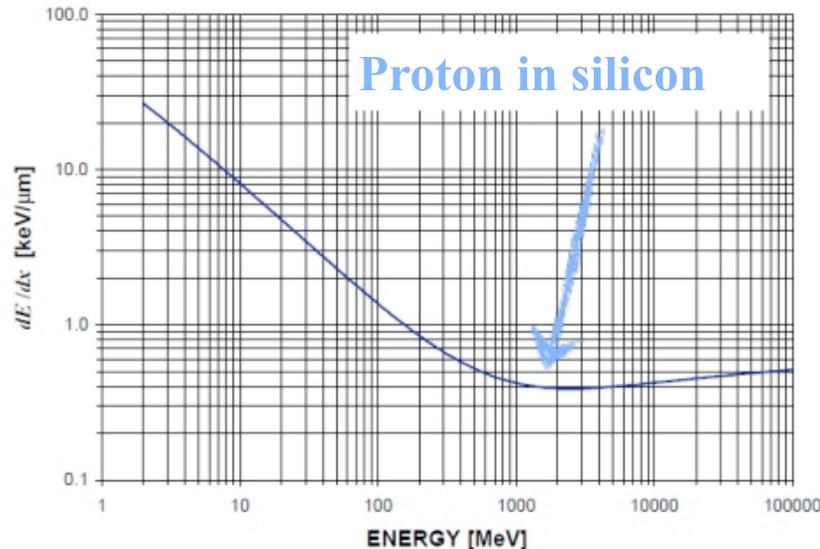
	Si	Ge	GaAs	CdTe	Diamant	SiC
band gap	1.12	0.67	1.42	1.56	5.48	2.99
energy for e - hole pair [eV]	3.6	2.9	4.2	4.7	13.1	6.9
e- for MIP (300 $\mu$ m)	24000	50000	35000	35000	9300	19000
Z	14	32	31+33	48+52	6	14+6

## Why is silicon used more often ?

- Silicon is the only material which can be produced in larger areas in high quality
- compare band gap to  $kT = 0.026$  eV at room temperature  $\rightarrow$  dark current under control
- high density compared to gases:  
 $\rho = 2.33 \text{ g/cm}^3$
- good mechanical stability
- large charge carrier mobility
- fast charge collection  $\delta t \sim 10 \text{ ns}$
- radiation tolerant

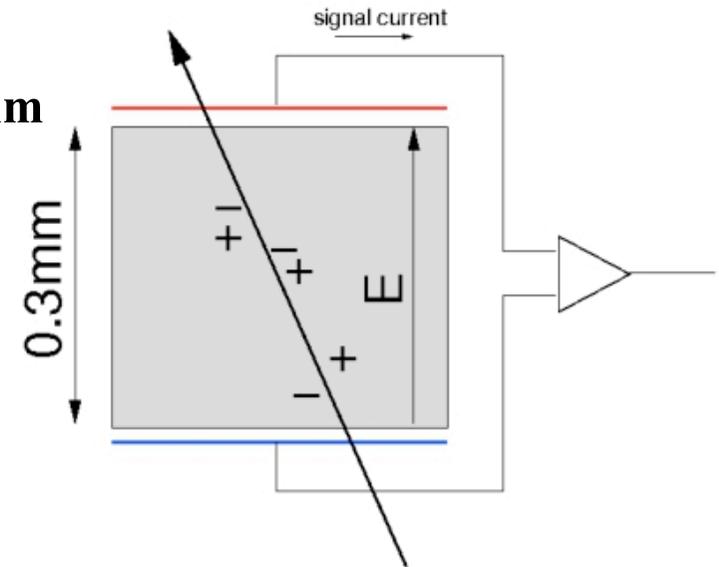


# Constructing a Detector



**Si detector:**

**Thickness: 0.3 mm**  
**Area: 1 cm<sup>2</sup>**



- mean ionization energy  $I_0 = 3.62 \text{ eV}$ ,
- mean energy loss per flight path of a mip  $dE/dx = 3.87 \text{ MeV/cm}$

**Signal of a mip in detector:**

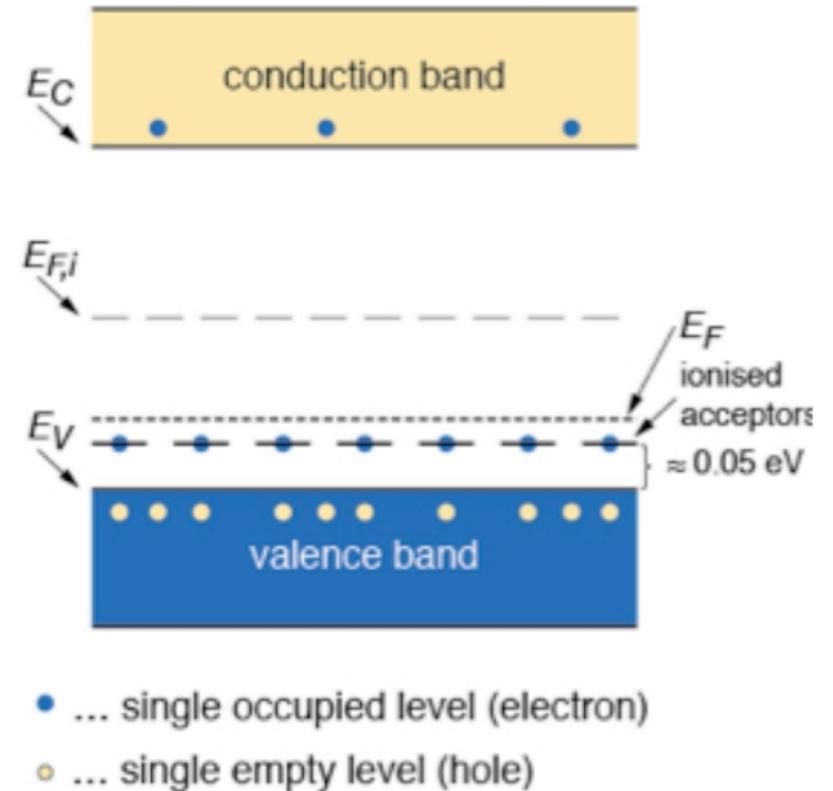
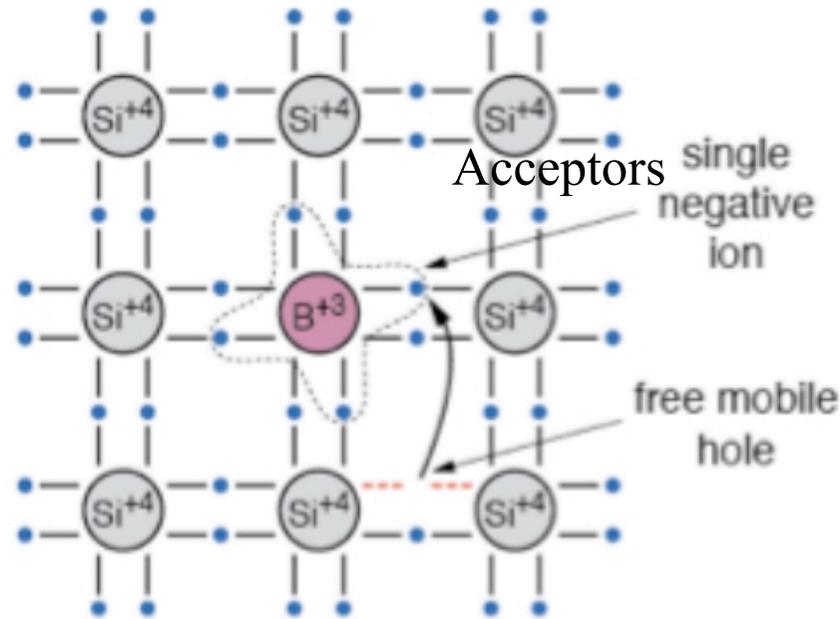
$$\frac{dE/dx \cdot d}{I_0} = \frac{3.87 \cdot 10^6 \text{ eV/cm} \cdot 0.03 \text{ cm}}{3.62 \text{ eV}} \approx 3.2 \cdot 10^4 \text{ e}^- \text{h}^+ \text{-pairs}$$

**Intrinsic charge carrier in a volume of same thickness and  $A=1 \text{ cm}^2$  ( $T = 300 \text{ K}$ ):**

$$n_i d A = 1.45 \cdot 10^{10} \text{ cm}^{-3} \cdot 0.03 \text{ cm} \cdot 1 \text{ cm}^2 \approx 4.35 \cdot 10^8 \text{ e}^- \text{h}^+ \text{-pairs}$$

**Result:** The number of thermally created  $\text{e}^- \text{h}^+$  -pairs (noise) is four orders of magnitude larger than the signal

# Doping Silicon

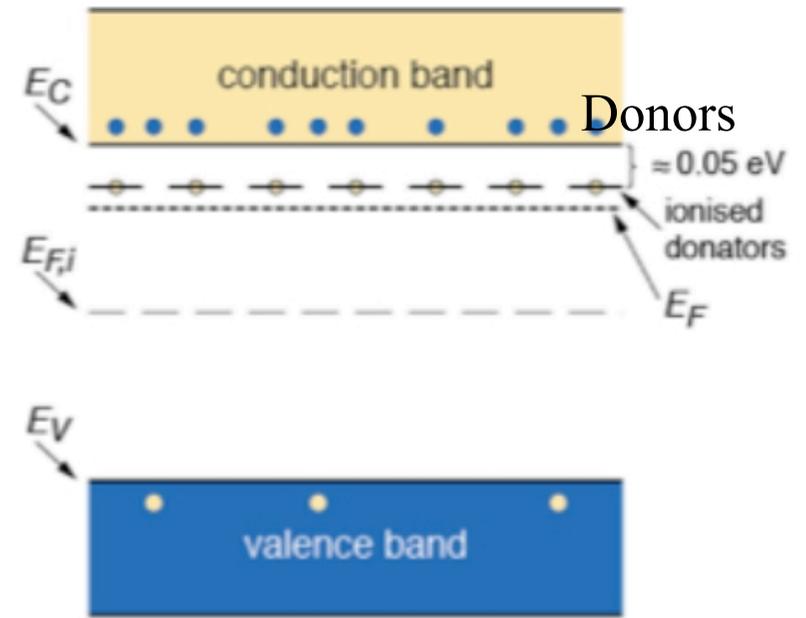
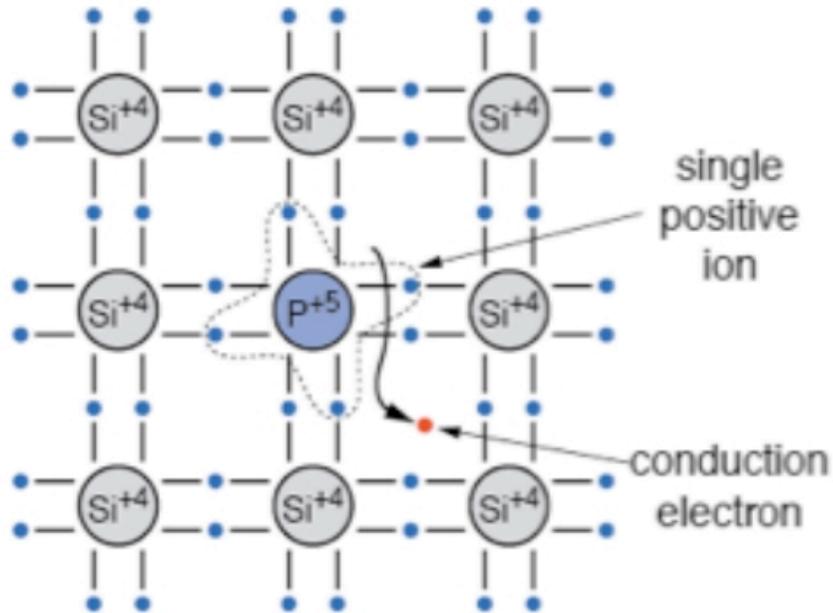


## p--type:

- In a p --type semiconductor, positive charge carriers (holes) are obtained by adding impurities of acceptor ions ( eg . Boron (type III)).
- Acceptors introduce energy levels close to valence band thus ‘absorb’ electrons from VB, creating holes ( $E_F$  closest to VB)

**Holes** are the majority carriers.

# Doping Silicon



● ... single occupied level (electron)

● ... single empty level (hole)

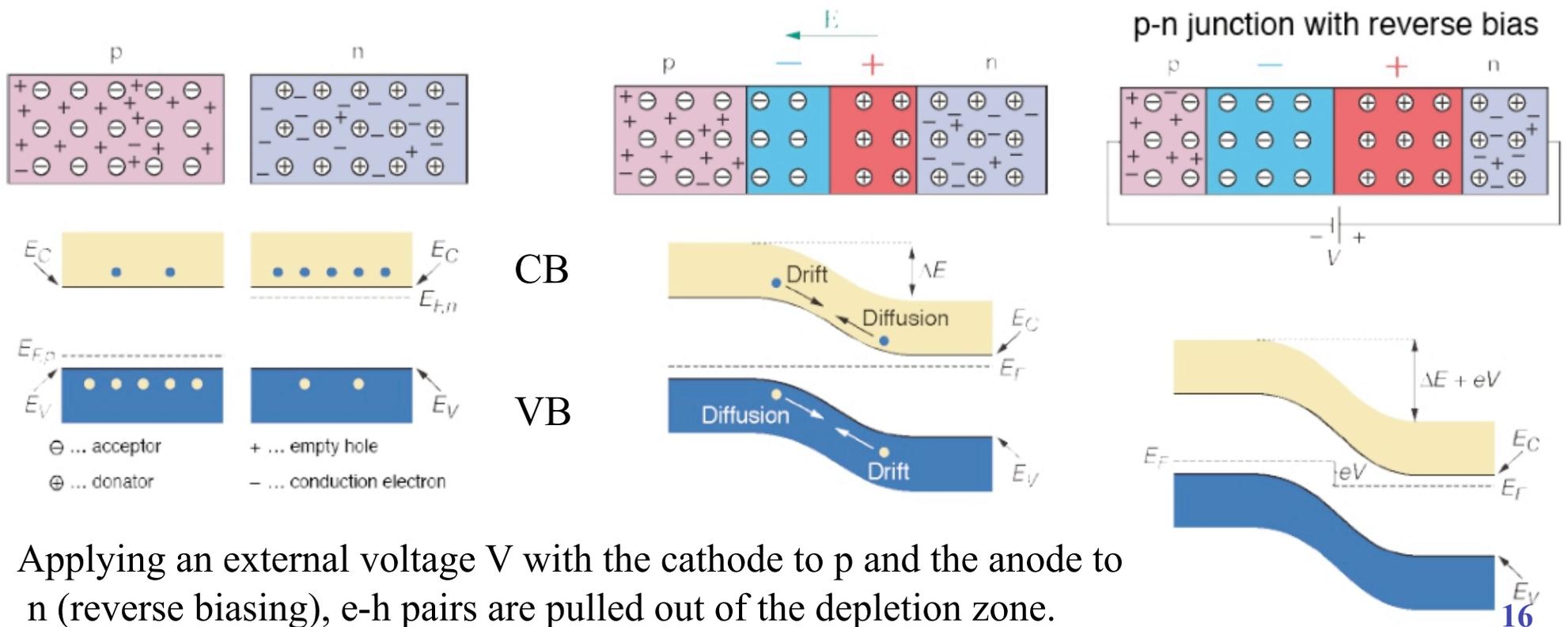
## n--type:

- In an n --type semiconductor, negative charge carriers (electrons) are obtained by adding impurities of donor ions ( eg . Phosphorus (type V))
- Donors introduce energy levels close to conduction band thus almost fully ionized ( $E_F$  closest to CB)

**Electrons** are the majority carriers.

# pn Junction

- At interface of a p-- type and n-type semiconductor the difference in the Fermi levels causes diffusion of excessive carriers to the other material until thermal equilibrium is reached. At this point the Fermi levels are equal.
- The remaining ions create a **space charge region** and an electric field stopping further diffusion.
- The stable space charge region free of charge carriers is called **depletion zone**.



Applying an external voltage  $V$  with the cathode to p and the anode to n (reverse biasing), e-h pairs are pulled out of the depletion zone.

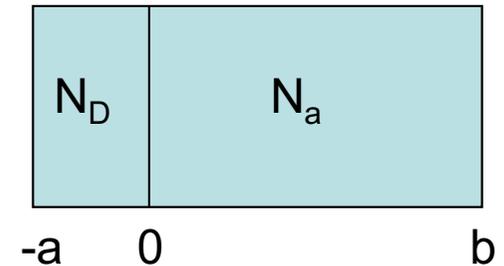
→ **larger depletion zone** → **suppress current across the junction**

# Depth of the Depletion Layer I

Poisson-Equation for the potential  $U(x)$  (1-dimensional for simplicity):

$$\frac{d^2U(x)}{dx^2} = \frac{-\rho(x)}{\epsilon\epsilon_0}$$

with  $E_x = -dU / dx \rightarrow \frac{dEx(x)}{dx} = \frac{\rho(x)}{\epsilon\epsilon_0}$



$$\rho(x) = \begin{cases} eN_D & \text{für } -a < x \leq 0 \\ -eN_A & \text{für } 0 < x \leq b \end{cases}$$

Asymmetric double layer with  $N_D$ ,  $N_A$  density of donor- and acceptor impurities.

Assumption:  $N_D \gg N_A$  and  $a < b$

Boundary conditions for electric field:

$$E_x(-a) = 0 = E_x(b)$$

1. Integration of Poisson equation with above boundary conditions

$$\rightarrow dU / dx = \begin{cases} -\frac{eN_D}{\epsilon\epsilon_0} (x+a) & \text{für } -a < x \leq 0 \\ +\frac{eN_A}{\epsilon\epsilon_0} (x-b) & \text{für } 0 < x \leq b \end{cases} \quad 17$$

# Depth of the Depletion Layer II

Boundary condition for the potential:

$$U(-a) = 0 \quad \text{und} \quad U(b) = -U_0 \quad \leftarrow \text{applied voltage}$$

2. Integration:

$$U(x) = \begin{cases} -\frac{eN_D}{2\epsilon\epsilon_0} (x+a)^2 & \text{für } -a < x \leq 0 \\ +\frac{eN_A}{2\epsilon\epsilon_0} (x-b)^2 - U_0 & \text{für } 0 < x \leq b \end{cases}$$

Use  $N_D a = N_A b$  and continuity at  $x=0$ :

$$b(a+b) = \frac{2\epsilon\epsilon_0 U_0}{eN_A}$$

For the strongly asymmetric case ( $N_D \gg N_A$ )  $b \gg a$  ( $b$ : thickness of p-doped layer)

$\rightarrow d = a + b \sim b \rightarrow$

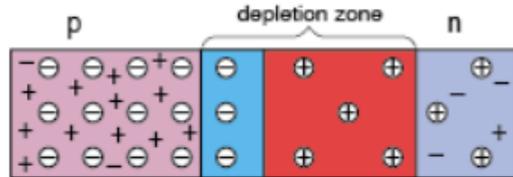
$$d = \sqrt{\frac{2\epsilon\epsilon_0 U_0}{eN_A}}$$

# The pn-Junction: Electric Field

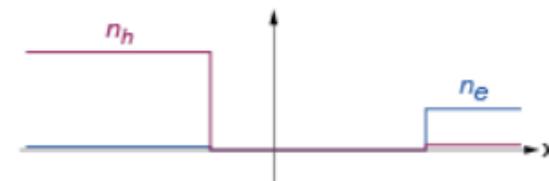
The highest field strength is then at  $x=0$ :

$$E_x(0) = \sqrt{\frac{2eN_A U_0}{\epsilon_0 \epsilon}} = \frac{2U_0}{d}$$

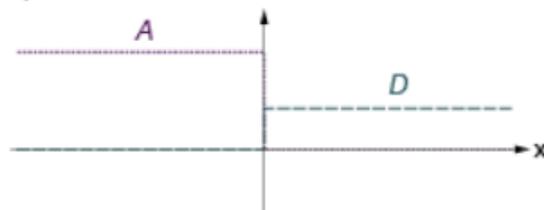
pn junction scheme



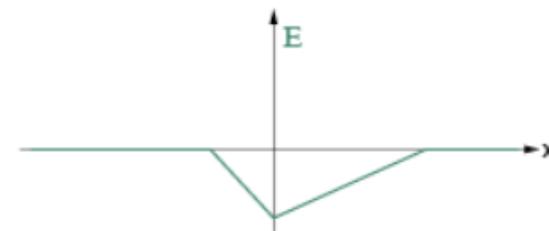
concentration of free charge carriers



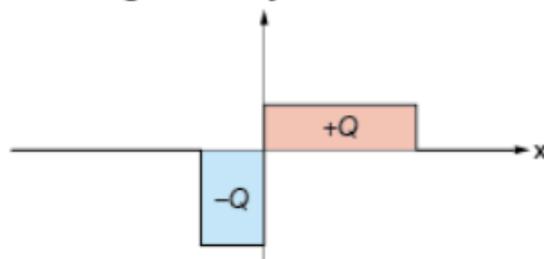
acceptor and donator concentration



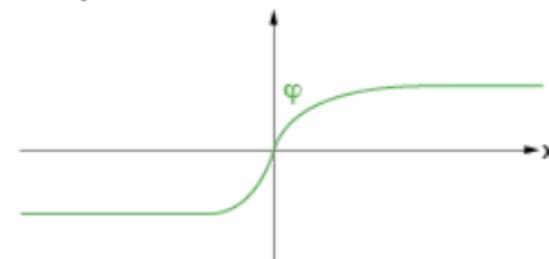
electric field



space charge density



electric potential



⊖ ... acceptor      ⊕ ... empty hole  
⊕ ... donator      - ... conduction electron

# Width of the depletion zone: Example

## > Effective doping concentration in typical silicon detector with p+-n junction

- $N_a = 10^{15} \text{ cm}^{-3}$  in p+ region
- $N_d = 10^{12} \text{ cm}^{-3}$  in n bulk.

## > Without external voltage:

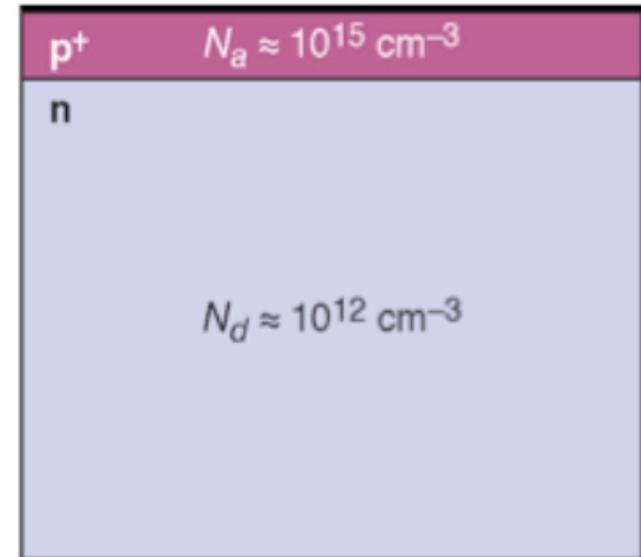
- $W_p = 0.02 \text{ } \mu\text{m}$
- $W_n = 23 \text{ } \mu\text{m}$

## > Applying a reverse bias voltage of 100 V:

- $W_p = 0.4 \text{ } \mu\text{m}$
- $W_n = 363 \text{ } \mu\text{m}$

## > Width of depletion zone in n bulk:

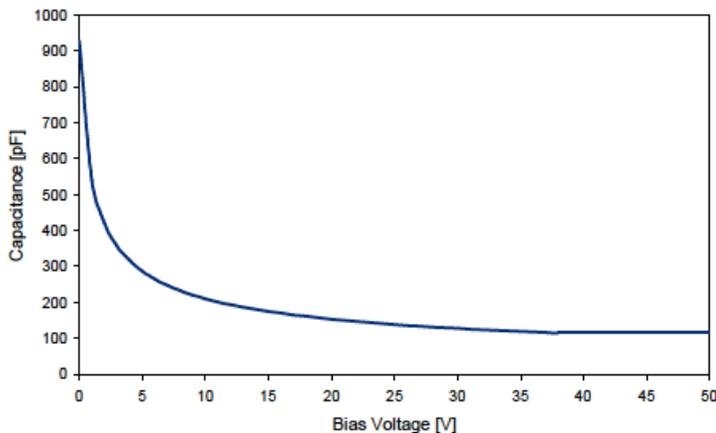
$$W \approx \sqrt{2\varepsilon_0\varepsilon_r\mu\rho|V|} \quad \text{with} \quad \rho = \frac{1}{e\mu N_{\text{eff}}}$$



$V$  ... External voltage  
 $\rho$  ... specific resistivity  
 $\mu$  ... mobility of majority charge carriers  
 $N_{\text{eff}}$  ... effective doping concentration

# Full Depletion Voltage and Doping Concentration

The capacitance vs. voltage characteristic of a diode can be used to determine the doping concentration of the detector material



$$C = A \sqrt{\frac{\epsilon q_e N}{2(V_b + V_{bi})}}$$

$A = \text{area}$

$N = \text{dopant concentration}$

$V_b = \text{bias voltage}$

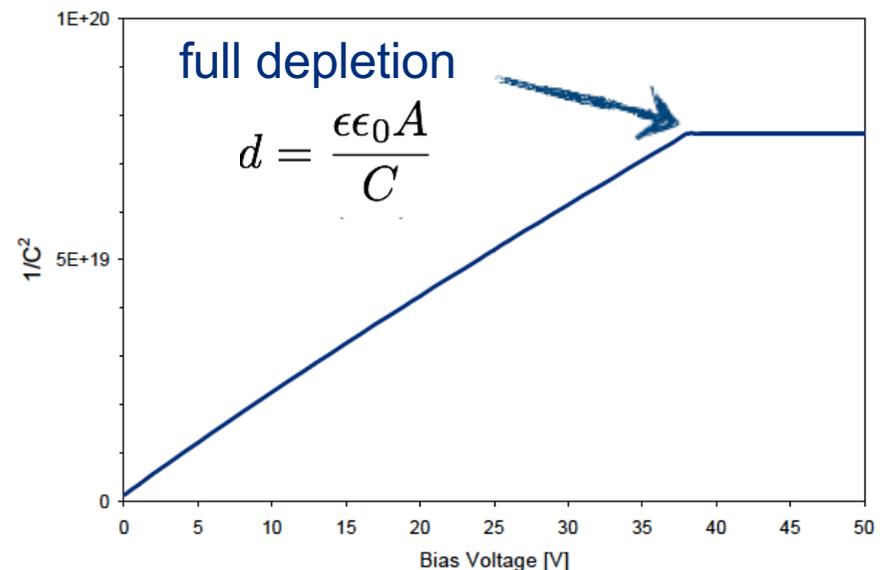
$V_{bi} = \text{built-in voltage}$

from this measurement the **dopant concentration** as a function of the diode depth is determined

$$N(x) = \frac{2}{\epsilon \epsilon_0 q_e A^2} \left( \frac{d \left( \frac{1}{C^2} \right)}{dV} \right)^{-1}$$

the dopant concentration defines the **electric field** in the diode

$$E(x) = \frac{q_0}{\epsilon \cdot \epsilon_0} \cdot \int N(x) \cdot dx$$

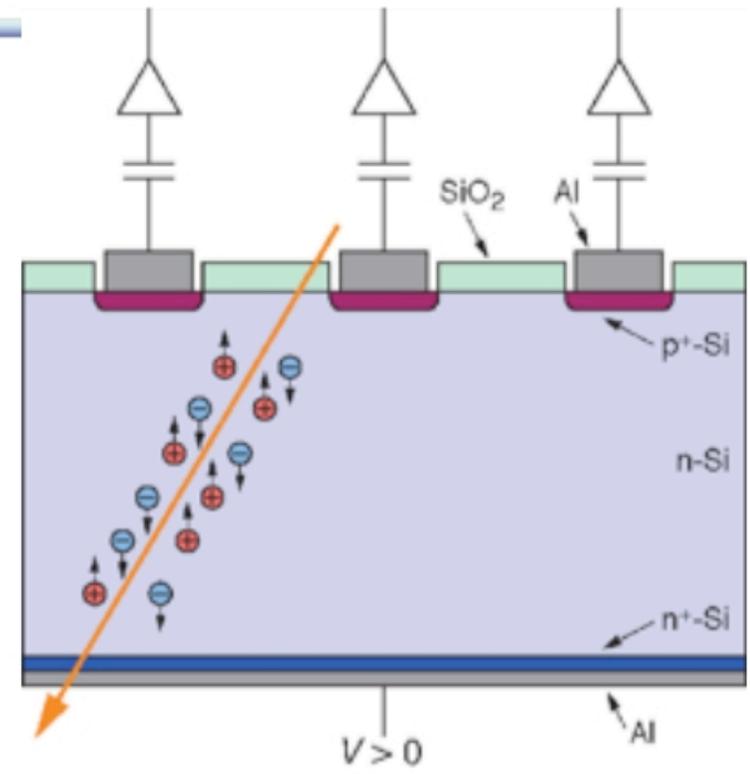


# Position Resolution -- Strip Detector

- Charge carrier drift to electrodes and induce signal
- By segmenting the implant we can reconstruct the position of the traversing particle in one dimension

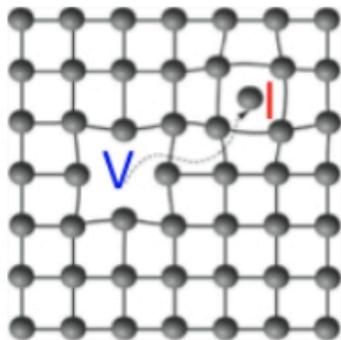
## Example : p<sup>+</sup>--in--n strip sensor:

- Strips are ( f.e.) Boron implants (p<sup>-</sup> type)
- Substrate is Phosphorous doped ( $\sim 2\text{--}10\text{ k}\Omega\text{cm}$ ) and  $\sim 300\mu\text{m}$  thick,  $V_{\text{dep}} < 200\text{V}$
- Backside Phosphorous implant to establish ohmic contact and to prevent early breakdown
- Highest field close to the collecting electrodes where most of the signal is induced
- Deposition of SiO<sub>2</sub> with a thickness of 100–200 nm between p<sup>+</sup> and aluminum strip
- **AC coupling** blocks leakage current from the amplifier



# Problem: Radiation Damage

- Radiation damage the silicon on atomic level significantly leading to macroscopic effect.
- **Bulk effects:** displacement damage and built up of crystal defects due to Non Ionizing Energy Loss (NIEL) **(main problem for sensors )**.  
unit : 1MeV equivalent neutron/cm<sup>2</sup> (up to 10<sup>15</sup> neq/cm<sup>2</sup> )

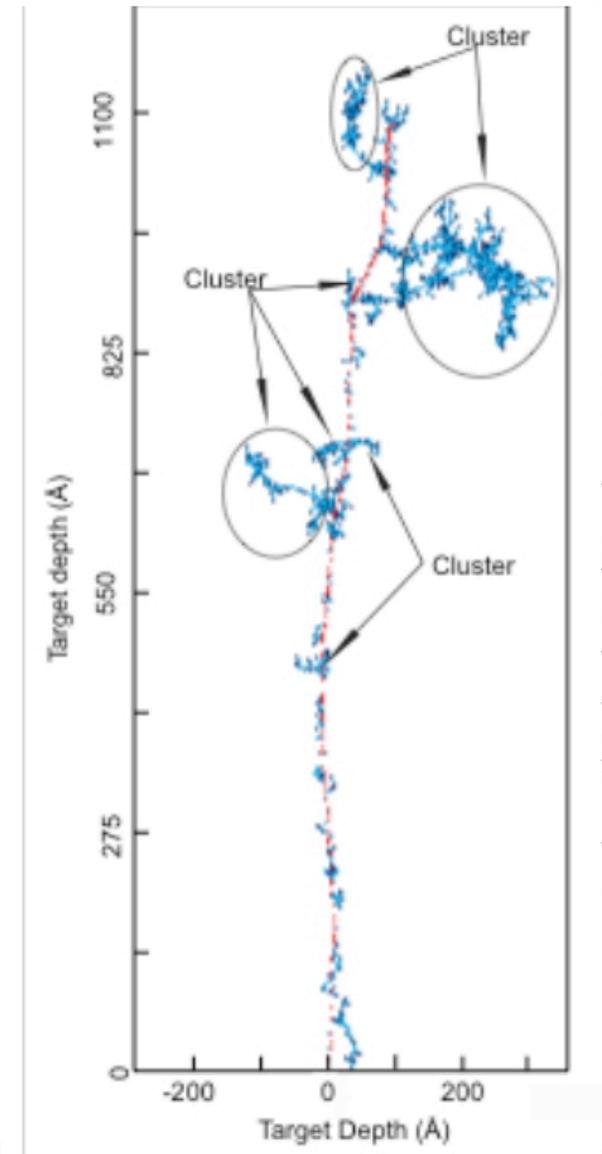


Defects composed of:  
**V**acancies and **I**nterstitials

Compound defects with impurities possible!

- **Surface effects:** Generation of charge traps due to ionizing energy loss (Total ionizing dose, TID) **( main problem for electronics)**.  
unit : Rad (up to 100 MRad)

very complex topic ....

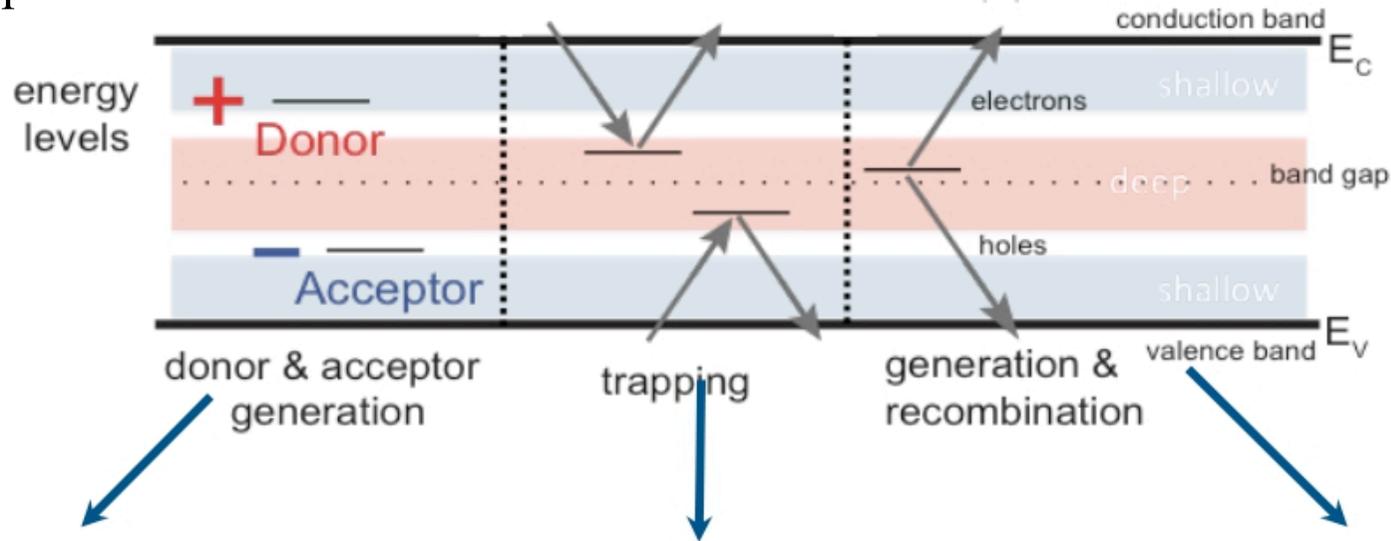


Simulation of 50 keV PKA  
damage cascade



# Radiation Damage: Bulk Defects

- Impact of defects on detector properties depends on defect level in band gap



**Change of effective doping concentration ( $N_{\text{eff}}$ )**

Increase of depletion voltage  
or Underdepleted operation

**Increased charge trapping**

Loss of signal (reduced charge collection efficiency)

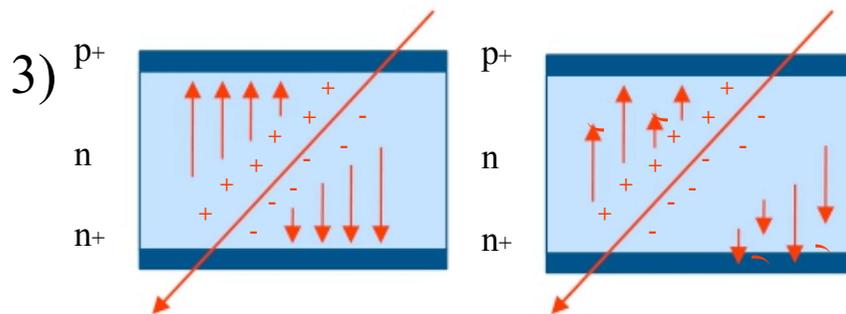
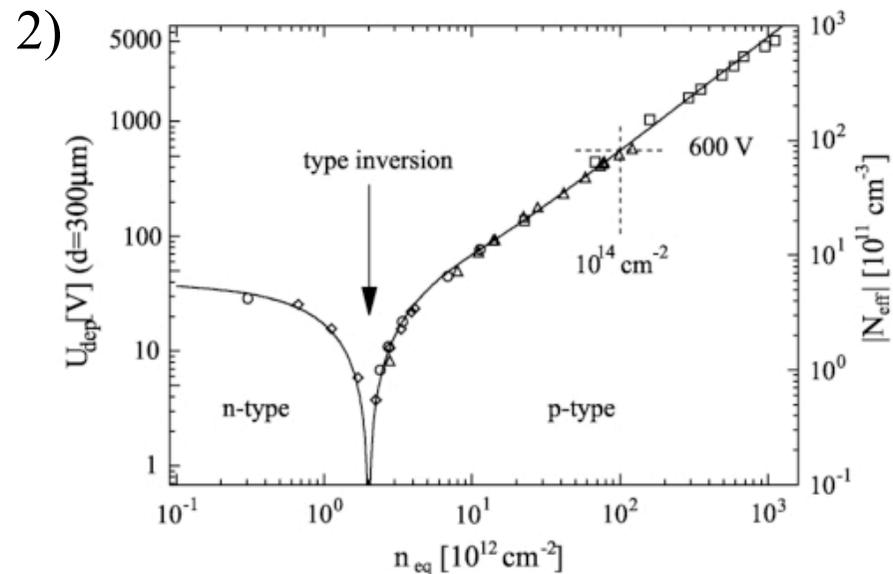
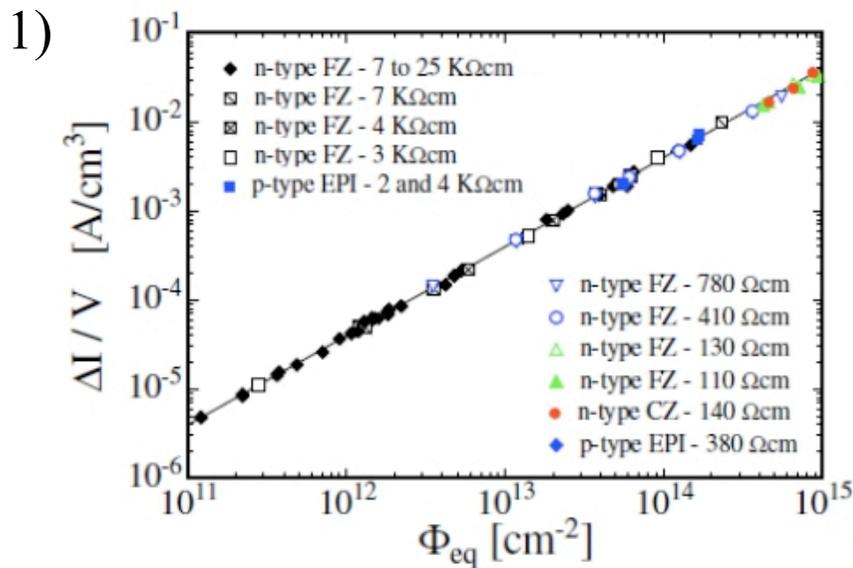
**Increase of leakage current**

higher shot noise  
thermal runaway

→ Cooling during operation helps!

# Consequences of Radiation Damage

- 1) direct excitation now possible  $\Rightarrow$  higher leakage current  $\Rightarrow$  more noise
- 2) can also contribute to space charge  $\Rightarrow$  higher  $V_{\text{bias}}$  necessary for full depletion
- 3) “charge trapping”, causing lower charge collection efficiency  $\Rightarrow$  lower signal



Charge trapping in defects

## Counter measures

- Geometrical: develop sensors that can withstand higher depletion voltages
- Thinner sensors (but FE electronics with higher sensitivity needed)
- Environment: sensor cooling ( -10 .. -20<sup>o</sup> C)
- Oxygen-- rich Si can help: depletion voltage **27**